Floating-Point C Extensions

X3J11 FP/IEEE Subcommittee Technical Report Final Report: Draft #2 WG14/N319, X3J11/94-003 January 6, 1994

Foreword

The Numerical C Extensions Group, NCEG, at its initial meeting in May 1989, identified support for IEEE floating-point arithmetic as one of its focus areas and organized a subgroup to produce a technical report. NCEG, now the ANSI working group X3J11.1, has had the benefit of both C language expertise and also IEEE floating-point expertise. It has included individuals with substantial experience with language extensions (albeit proprietary) for IEEE floating-point. And, following the C language standardization, NCEG has had a stable, well defined host for its extensions. Thus NCEG has had a unique opportunity to solve this long-standing problem.

When IEEE binary floating-point standard 754 became an official standard in July 1985, 26 months before the radix-independent standard 854, several IEEE implementations were already shipping. Now virtually all new floating-point implementations conform to the IEEE standards—at least in format, if not to the last detail. Although these standards have been enormously successful in influencing hardware implementation, many IEEE features remain impractical or unavailable for use by programmers. The IEEE standards do not include language bindings—part of the cost of delivering the basic standard in a timely fashion. The ANSI C committee attempted to eliminate conflicts with IEEE arithmetic, but did not specify IEEE support. In the meantime, particular companies have defined their own IEEE language extensions and libraries [4, 8, 10]; not surprisingly, lack of portability has impeded programming for these interfaces.

The initial version of this document, in August 1989, was organized foremost as a specification for IEEE implementations, with notes for other implementations. However, from the beginning, substantial portions of the specification were not specific to IEEE floating-point. For broader utility the document was reorganized as a general floating-point specification with additional specification for IEEE implementations.

NCEG mailings have included twelve drafts of this document, which have been reviewed to varying degrees by NCEG's FP/IEEE subgroup, NCEG as a whole, and numerous other interested parties. Proprietary extensions for IEEE support have provided prior art for many features. Substantial portions of the specification have been implemented in both developmental and commercial compilers and libraries.

An earlier draft of "Floating-Point C Extensions" (X3J11.1/92-040) was distributed for preliminary review to various professional organizations, including X3J11, WG14, X3J16/WG21, X3T2, and X/Open. The subsequent draft (X3J11.1/93-001) was distributed for public comment. NCEG approved the next draft (X3J11.1/93-028, WG14/N291, X3J11/93-037) for forwarding to X3J11 as its FP/IEEE technical report. At its December 1993 meetings, NCEG approved the minor changes listed in "Changes to Floating-Point C Extensions" (WG14/N320, X3J11/94-004), which are incorporated into this, the second draft of the technical report (WG14/N319, X3J11/94-003). Comments accompanying the NCEG votes on the motion to forward X3J11.1/93-028 to X3J11 are attached following the main document below.

People who have made especially substantial contributions to this document include, in alphabetical order: Jerome Coonen, Bill Gibbons, David Hough, Rex Jaeschke, W. Kahan, Clayton Lewis, Stuart McDonald, Colin McMaster, Rick Meyers, David Prosser, and Fred Tydeman.

Others who have provided invaluable contributions, reviews, or administrative help include, in alphabetical order: Joel Boney, Norris Boyd, Larry Breed, Walter Bright, W. J. Cody, Elizabeth Crockett, Karen Deach, James Demmel, Fred Dunlap, Clive Feather, Yinsun Feng, Samuel Figueroa, James Frankel, Scott Fraser, David Gay, Eric Grosse, Ron Guilmette, Doug Gwyn, Bill Homer, Kenton Hanson, Paul Hilfinger, Martha Jaffe, Bob Jervis, David Keaton, Earl Killian, David Knaak, John Kwan, Roger Lawrence, Tom MacDonald, Michael Meissner, Randy Meyers, Antonine Mione, Stephen Moshier, Jon Okada, Conor O'Neill, Tom Pennello, Tim Peters, Thomas Plum, Sanjay Poonen, Pat Ricci, Ali Sazegari, Roger Schlafly, Steve Sommars, Richard Stallman, Linda Stanberry, Gordon Sterling, Bill Torkelson, and Terrence Yee.

This document benefited from the author's previous experience with Apple Computer, Inc.'s numerics and languages groups, developing the Standard Apple Numerics Environment (SANE) and its various language bindings.

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January 6, 1994

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1. Introduction

15 1.1 Purpose

This document specifies:

1. a set of Standard C extensions, suitable for most implementations, and designed to facilitate a wide range of numerical programming;

2. a further set of extensions and definitions, suitable for implementations that support IEEE floating-point standards 754 and 854, and designed to provide full access to the features of those standards—allowing access also to similar features in non-IEEE implementations.

This document is intended for incorporation into a Technical Report of the Numerical C Extensions Group (NCEG/X3J11.1).

30 **1.2 Scope**

The specifications of this document, while extending Standard C, still lie within the scope of that standard ([17] §4.2; [1] §1.2).

- 35 This document does not:
 - 1. describe Standard C, except where it relates to extensions or subtleties of implementation, but instead refers implicitly to the Standard C documents [17], [1];
- 2. describe IEEE floating-point per se, but instead refers implicitly to the 754 and 854 standards documents;
 - 3. address other NCEG areas, such as complex arithmetic, which are expected to accommodate IEEE standard arithmetic.

1.3 References

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- 20. "An Argument of Apple's Support of the Extended Floating-Point Type", Jim Thomas and Jerome Coonen (September 14, 1989)—NCEG 89-037.
- 21. C* Language Reference Manual, James L. Frankel, Draft Technical Report, Thinking Machines Corporation (May 16, 1991)—NCEG 91-023.
 - 22. "Augmenting a Programming Language with Complex Arithmetic", W. Kahan and J. W. Thomas (November 15, 1991)—NCEG 91-039.
- 15 23. "Algorithm XXX: Specfun—A Portable Package of Special Functions and Test Drivers", W. J. Cody (work in progress).
 - 24. "Floating-Point C Extensions", Jim Thomas (August 10, 1991)—NCEG 91-028.
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1.4 Organization of Document

The major subsections are:

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1. this introduction:

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- 2. characteristics of the translation and execution environments;
- 30 3. language syntax, constraints, and semantics;
 - 4. library facilities;
- A. summary of language syntax extensions;
- B. optimization notes;
 - C. summary of library facilities;
- 40 D. implementation limits;
 - E. documentation guide for operators and functions;
 - F. specification of library facilities for IEEE implementations.
 - Sections that can be regarded as extending or modifying a particular section of the Standard C documents are marked with the section numbers from the ISO C [17] and ANSI C [1] documents, for example
- 50 3.1.2 Floating constants (ISO §6.1.3.1; ANSI §3.1.3.1)

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Rationale, in smaller font size, accompanies sections that are controversial or where further explanation seems needed. Subsections entitled "For IEEE Implementations" contain specification that applies specifically to implementations that support features of the IEEE floating-point standards.

As in the IEEE floating-point standards, use of the word shall signifies that which is obligatory for conformance; use of the word should signifies that which is strongly recommended, though impractical for certain implementations.

1.5 Definition of Terms

- Double—the IEEE floating-point standards' double data format. Written in program-text style, double refers to the Standard C data type. Where noted, double refers locally to both IEEE and also non-IEEE double precision formats.
- Double-based architecture—a floating-point architecture designed to produce primarily double format results.
- Evaluation format—the format used to represent the result of an expression. It may be wider than the semantic type of the expression.
- Exception flag—a flag signifying that a floating-point exception has occurred. IEEE implementations support overflow, underflow, invalid, divide-by-zero, and inexact exception flags.
- Expression evaluation method—a method for determining the evaluation formats for expressions.
- Extended—the IEEE floating-point standards' double-extended data format. Extended refers to both the common 80-bit and so-called quadruple 128-bit IEEE formats. Where noted, extended refers locally to both IEEE and also non-IEEE formats that are wider than double.
- Extended-based architecture—a floating-point architecture designed to produce primarily extended format results.
 - Flag—see exception flag.
- Floating-point environment—collectively all floating-point status flags and control modes
- Floating-point standards—specifically IEEE Standard for Binary Floating-Point Arithmetic (ANSI/IEEE Std 754-1985) and IEEE Standard for Radix-Independent Floating-Point Arithmetic (ANSI/IEEE Std 854-1987).
- IEEE implementation—an implementation that conforms to one or both of the IEEE floating-point standards. See *floating-point standards*.
- Implementation-defined behavior—behavior that depends on the characteristics of the implementation and that each implementation shall document. (As in Standard C.)

• Mode—short for floating-point control mode.

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- NaN—in a floating-point format, an encoding that signifies *Not-a-Number*. In this document the term NaN generally denotes quiet NaNs.
- Normal number—a nonzero, finite number that is not subnormal. (As in IEEE standard 854.)
- Quiet NaN—a NaN that propagates through almost every arithmetic operation without raising an exception.
 - Rounding direction mode—a dynamic mode that controls the style of rounding used by floating-point operations. For IEEE implementations the rounding directions are upward, downward, toward zero, and to nearest.
 - Rounding precision mode—a dynamic or static mode that controls the precision to which floating-point operations round their results.
 - Signaling NaN—a NaN that generally raises an exception when occurring as an arithmetic operand. This specification does not cover signaling NaNs.
 - Single—the IEEE floating-point standards' single data format. Where noted, single refers locally to both IEEE and also non-IEEE single precision formats.
- Single/double architecture—a floating-point architecture designed to produce with like efficiency either single or double format results, with any extended arithmetic being substantially slower.
- Single/double/extended architecture—a floating-point architecture designed to produce with like efficiency either single, double, or extended results.
 - Standard C—the C language standard, International Standard ISO/IEC 9899 and American National Standard Programming Language C.
- Subnormal number—a nonzero floating-point number whose exponent is the format's minimum and whose leading significand digit is zero. (As in IEEE standard 854.)
 - Undefined behavior—behavior, for an erroneous program or erroneous data, for which this specification imposes no requirement. (As in Standard C.)
 - Unspecified behavior—behavior, for a correct program and correct data, for which this specification imposes no requirement. (As in Standard C.)
- Warning—a translation-time message alerting the user when reasonable or common expectations for a formally correct program may not be met.

1.6 Compliance

In order to comply as an implementation supporting IEEE standard floating-point, an implementation must conform to one, or both, of the IEEE standards 754 and 854—which ones is implementation-defined.



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2. Environment

Any floating-point status flags and control modes supported by the implementation are here referred to collectively as the *floating-point environment*. Programs that test flags or run under non-default modes must do so under the effect of an enabling fenv_access pragma.

*pragma fenv_access on-off-switch

on-off-switch: one of:
on off default

can occur outside external declarations and takes effect from its occurrence until another fenv_access pragma is encountered, or until the end of the translation unit. The effect of this pragma appearing inside an external declaration is undefined. If part of a program tests flags or runs under non-default mode settings, but is not under the effect of an enabling fenv_access pragma, then the behavior of that program is undefined. (Part of a program is under the effect of an enabling fenv_access pragma if that part is translated while the state of the pragma is on.) The default state (on or off) for the pragma is implementation-defined. (§4.4 specifies facilities for accessing the floating-point environment.)

The floating-point environment as defined here includes only execution-time modes, not the myriad of possible translation-time options that may affect a program's results. Examples of such translation-time options include: chopped or rounded multiplication on CRAY Y-MP systems, D or G format for VAX, and fast or correctly-rounded divide on the Intel 860. Each option's implementation-defined or deviant properties, relative to this specification, should be well documented.

The purpose of the fenv_access pragma is to allow certain optimizations, namely global common subexpression elimination, code motion, and constant folding, that could subvert the testing of flags and changing of modes. For example, in

```
double x;
void f(double);
void g(double);
...
f(x + 1);
g(x + 1);
...
```

the function f might depend on status flags set as a side effect of the first x + 1. The second x + 1 might depend on control modes set as a side effect of the function call f. The imposed teliporal ordering would require two evaluations of x + 1. This specification says that if in fact the program tests flags or changes modes through the call to f, it must so declare with an enabling fenv_access pragma. In general, if the state of fenv_access is off then the translator can assume that default modes are in effect.

The user model is supported by certain programming conventions:

1. A function call must not alter its caller's modes, clear its caller's flags, nor depend on the state of its caller's flags unless the function is so documented. (To do otherwise would be extremely dangerous, irrespective of this specification.)

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otherwise, or unless the function is known not to use floating-point. 3. A function call is assumed to have the potential of raising floating-point exceptions, 5 unless its documentation promises otherwise, or unless the function is known not to use floating-point. With these conventions a programmer can assume default modes, or ignore them altogether, safely and without code or intellectual overhead. Responsibilities, and ordinarily modest 10 overhead, associated with accessing the floating-point environment fall entirely on the programmer or program that does so. No standard library function, except those in <fenv.h>, tests or clears its caller's flags or changes its caller's modes. 15 Libraries are encouraged to document their use, or non-use, of floating-point and their raising of floating-point exceptions. The performance of code under the effect of an enabling fenv_access pragma may well be 20 important; in fact, an algorithm may access the floating-point environment specifically for performance. The implementation should optimize as aggressively as the fenv_access pragma allows. (See §B.1.) An implementation could simply honor the floating-point environment in all cases and 25 ignore the pragma. Dynamic vs static modes Dynamic modes are potentially problematic because 30 1. the programmer may have to defend against undesirable mode settings—which imposes intellectual, as well as time and space, overhead. 2. the translator may not know which mode settings will be in effect or which functions 35 change them at execution time—which inhibits optimization. This proposal attempts to address these problems without changing the dynamic nature of the modes. 40 An alternate approach would have been to present a model of static modes, with explicit utterances to the translator about what mode settings would be in effect. This would have avoided any uncertainty due to the global nature of dynamic modes or the dependency on unenforced conventions. However, some essentially dynamic mechanism still would have been needed in order to allow functions to inherit (honor) their caller's modes. The IEEE 45 standards require dynamic rounding direction modes. For the many architectures that maintain these modes in control registers, implementation of the static model would be more costly. Also, Standard C has no facility, other than pragmas, for supporting static modes. 50 An implementation on an architecture that provides only static control of modes, for example through opword encodings, still could support the dynamic model, by generating multiple code streams with tests of a private global variable containing the mode setting. Only modules under an enabling fenv_access pragma would need such special treatment. To further limit the problem, the implementation might employ additional pragmas 55 specifically to indicate where non-default modes would be admissible.

2. A function call is assumed to require default modes, unless its documentation promises

For IEEE Implementations

The IEEE floating-point standards require that an implementation support certain status flags and control modes.

The exception flags—invalid, overflow, underflow, divide-by-zero, and inexact—can be queried at execution time to determine whether a floating-point exception has occurred since the beginning of execution or since its flag was explicitly cleared. (The flags are sticky.)

The rounding direction modes—to-nearest, toward-zero, upward (toward $+\infty$), and downward (toward $-\infty$)—can be altered at execution time to control the rounding direction for floating-point operations.

The rounding precision modes cause a system whose results are always double or extended to shorten the precision of its results, in order to mimic systems that deliver results to single or double precision. Some systems need not implement rounding precision modes—see §4.4.2.

The traps recommended by the IEEE floating-point standards require modes for enabling and disabling. Trap-enable modes lie outside the scope of this document.

2.1 Translation

An implementation should provide a warning for each translation-time floating-point exception, other than inexact. The implementation shall document all mode settings that affect the behavior of translation-time arithmetic.

For IEEE Implementations

30 During translation the IEEE standard default modes are in effect:

rounding direction:

to-nearest

rounding precision:

results not shortened

trapping:

all traps disabled

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An implementation is not required to provide a facility for altering the modes for

ranslation-time arithmetic, or for making exception flags from the translation available to the executing program. The language and library provide facilities to cause floating-point operations to be done at execution time, when they can be subjected to varying dynamic modes and their exceptions detected. The need does not seem sufficient to require similar facilities for translation.

2.2 Execution

45 2.2.1 Startup

At program startup any floating-point modes are initialized as for translation-time arithmetic. The implementation shall document all startup mode settings that affect the behavior of arithmetic.

This promotes consistency between translation- and execution-time computations.

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For IEEE Implementations

At program startup the floating-point environment is initialized as prescribed by the IEEE floating-point standards:

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exception flags: all clear rounding direction: to-nearest

rounding precision: results not shortened

trapping: all traps disabled

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2.2.2 Changing the environment

Operations defined in ISO §6.3 (ANSI §3.3) and functions and macros defined for standard libraries change flags and modes just as indicated by their specification (which may include conformance to standards); they do not change flags or modes (so as to be detectable by the user) in any other cases.

2.3 Environmental Limits

20 2.3.1 Characteristics of floating types (ISO §5.2.4.2; ANSI §2.2.4.2)

The value of the Standard C macro

FLT_ROUNDS

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is dynamically determined to represent the effective rounding direction.

Thus IEEE implementations, and any others that allow changing the rounding direction at execution time, must implement FLT_ROUNDS as an execution-time inquiry, not as a constant (when the state of fenv_access is on).

This specification augments <float.h> with two macros that characterize the evaluation method (§3.2.3.1) for evaluating floating-point expressions. The minimum evaluation format is characterized by the value of _MIN_EVAL_FORMAT:

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- 0 float
- 1 double
- 2 long double
- Whether widest-need evaluation is performed is characterized by _widest_need_eval:
 - 0 no
 - 1 yes

If the minimum evaluation format is long double then the value of _WIDEST_NEED_EVAL is irrelevant.

The values _MIN_EVAL_FORMAT and _WIDEST_NEED_EVAL need not be constants.

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An implementation that provides alternate expression evaluation methods must assure that translation-time evaluation of _MIN_EVAL_FORMAT and _WIDEST_NEED_EVAL reflects the current one.

3. LANGUAGE

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3.1 Lexical Elements (ISO §6.1; ANSI §3.1)

5 3.1.1 Types (ISO §6.1.2.5; ANSI §3.1.2.5)

The long double type should have strictly more precision than double which should have at least twice the number of digits of precision as float. If not, the implementation should emit a warning when processing a translation unit that uses distinct floating types with the same precision.

This facilitates porting code that, intentionally or not, depends on differences in type widths. Many results are exact or correctly rounded when computed with twice the number of digits of precision as the data. For example, the calculation

float d, x, y, z, w; d = (double) x * y - (double) z * w;

yields a correctly rounded determinant if double has twice the precision of float and the individual operations are correctly rounded. (The casts to double are unnecessary if the minimum evaluation format is double or long double—see §3.2.3.1.)

For IEEE Implementations

The C floating types match the IEEE standard floating-point formats as follows:

C type
float single
double double
long double extended, else a non-IEEE extended format, else
double

Any non-IEEE extended format, used as the long double format for an IEEE implementation, has more precision than IEEE double and at least the range.

Minimal conformance to the IEEE floating-point standards does not require a format wider than single. The narrowest C double type allowed by Standard C (ISO §5.2.4.2; ANSI §2.2.4.2) is wider than IEEE single, and wider than the minimum IEEE single-extended format. (IEEE single-extended is an optional format intended only for those implementations that don't support double; it has at least 32 bits of precision.) Both Standard C and the IEEE standards would be satisfied if float were IEEE single and double were an IEEE single-extended format with at least 35 bits of precision. However, this specification goes slightly further by requiring double to be IEEE double rather than just a wide IEEE single-extended.

The primary objective of the IEEE part of this specification is to facilitate writing portable code that exploits the IEEE floating-point standards, including their standardized single and double data formats. Bringing the C data types and the IEEE standard formats into line advances this objective.

This specification accommodates what are expected to be the most important IEEE floating-point architectures for general C implementations—see §3.2.3.

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Because of Standard C's bias toward double, extended-based architectures might appear to be better served by associating the C double type with IEEE extended. However, such an approach would not allow standard C types for both IEEE double and single and would go against current industry naming, in addition to undermining this specification's portability goal. Other features in this document, for example the type definitions float_t and double_t (defined in §4.3), are intended to allow effective use of architectures with more efficient, wider formats.

The long double type is not required to be IEEE extended because

- 1. some of the major IEEE floating-point architectures for C implementations do not support extended,
- 2. double precision is adequate for a broad assortment of numerical applications, and
- 3. extended is less standard than single or double in that only bounds for its range and precision are specified in IEEE standard 754.
- For implementations without extended in hardware, non-IEEE extended arithmetic written in software, exploiting double in hardware, provides some of the advantages of IEEE extended but with significantly better performance than true IEEE extended in software. [20] explains advantages of extended precision.
- Specification for a variable-length extended type—one whose width could be changed by the user—was deemed premature. However, not unduly encumbering experimentation and future extensions, for example for variable length extended, is a goal of this specification.

Narrow-format Implementations

Some C implementations, namely ones for digital signal processing, provide only the IEEE floating-point standards' single format, possibly augmented by single-extended, which may be narrower than IEEE double or Standard C double, and possibly further augmented by double in software. These non-conforming implementations might generally adopt this specification, though not matching its requirements for types.

One approach would be: match Standard C float with single; match Standard C double with single-extended, else single; and match Standard C long double with double, else single-extended, else single. Then most of this specification could be applied straightforwardly. Users should be clearly warned that the types may not meet expectations.

Another approach would be to refer to a single-extended format as long float and then not recognize any C types not truly supported. This would provide ample warning for programs requiring double. The translation part of porting programs could be accomplished easily with the help of type definitions. In the absence of a double type, most of this specification for double could be adopted for the long float type. Having distinct types for long float and double, previously synonyms, requires more imagination.

3.1.1.1 NaNs

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Floating types may support NaN (Not-a-Number) values, which do not represent numbers. A NaN that generally raises an exception when encountered as an operand of arithmetic operations is called a signaling NaN, and the operation is said to trigger the signaling NaN; this document does not define the behavior of signaling NaNs. A NaN that behaves predictably and does not raise exceptions in arithmetic operations is called a quiet NaN; this document uses the term NaN to denote quiet NaNs.

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The IEEE floating-point standards specify quiet and signaling NaNs, but these terms can be applied for some non-IEEE implementations as well—for example, the VAX reserved operand and the CDC and CRAY indefinite qualify as signaling NaNs. In IEEE standard arithmetic, operations that trigger a signaling NaN argument generally return a quiet NaN result provided no trap is taken; neither traps nor any other facility for signaling NaNs is required. True support for signaling NaNs implies restartable traps, such as the optional traps specified in the IEEE floating-point standards.

The primary utility of quiet NaNs—"to handle otherwise intractable situations, such as providing a default value for 0.0/0.0" [11]—can be supported through straightforward extensions to C. See §3.3.2, 4.2.1.2, 4.2.2.1-2, 4.3, 4.3.9.2.

Other applications of NaNs may prove useful. Available parts of NaNs have been used to encode auxiliary information, for example about the NaN's origin [4]. Signaling NaNs are good candidates for filling uninitialized storage; and their available parts could distinguish uninitialized floating objects. IEEE signaling NaNs and trap handlers potentially provide hooks for maintaining diagnostic information or for implementing special arithmetics.

However, C support for signaling NaNs, or for auxiliary information that could be encoded in NaNs, is problematic. Trap handling varies widely among implementations. Implementation mechanisms may trigger signaling NaNs, or fail to, in mysterious ways. The IEEE floating-point standards require that NaNs propagate, but not all implementations faithfully propagate the entire contents. And even the IEEE standards fail to specify the contents of NaNs through format conversion, which is pervasive in some C implementation mechanisms. For these reasons this document does not define the behavior of signaling NaNs nor specify the interpretation of NaN significands.

[24], a previous version of this document, contains specification for signaling NaNs. It could serve as a guide for implementation extensions in support of signaling NaNs.

3.1.2 Floating constants (ISO §6.1.3.1; ANSI §3.1.3.1)

Floating constants are converted to their internal representation at translation time. Each constant is represented in a format (perhaps wider than required by the constant's type) determined by the effective expression evaluation method (§3.2.3.1). The resulting values from translation-time conversion of (valid) floating constants match those from execution-time conversion with default rounding modes by library functions, like strtod. See §4.2.1.2.

Note that since floating constants are converted to appropriate internal representations at translation time, default rounding direction and precision will be in effect and execution-time exceptions will not be raised, even under the effect of an enabling fenv_access pragma. Library functions, for example strtod, provide execution-time conversion of decimal strings.

3.1.2.1 Hexadecimal floating constants (ISO §6.1.3.1, 6.1.8; ANSI §3.1.3.1, 3.1.8)

The Standard C *floating-constant* syntax is augmented to include hexadecimal floating constants.

Syntax

floating-constant:

5 hexadecimal-floating-constant

hexadecimal-floating-constant:

0x hexadecimal-fractional-constant binary-exponent-part floating-suffixopt

ox hexadecimal-fractional-constant binary-exponent-part floating-suffixopt

0x hexadecimal-digit-sequence binary-exponent-part floating-suffixopt

ox hexadecimal-digit-sequence binary-exponent-part floating-suffixopt

hexadecimal-fractional-constant:

hexadecimal-digit-sequenceopt hexadecimal-digit-sequence

hexadecimal-digit-sequence

hexadecimal-digit-sequence:

hexadecimal-digit

hexadecimal-digit-sequence hexadecimal-digit

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binary-exponent-part:

p signopt digit-sequence

P signopt digit-sequence

The binary exponent gives a decimal integer representing a power of 2. If FLT_RADIX is a power of two, hexadecimal floating constants are correctly rounded. The implementation shall emit a warning if a hexadecimal constant cannot be represented exactly in its evaluation format (see §3.2.3.1). Further accuracy specification for the conversion of hexadecimal floating constants to internal format is implied by the specification for the strtod functions (§4.2.1.2).

In order to accommodate hexadecimal floating constants, the Standard C syntax for preprocessing numbers (ISO §6.1.8; ANSI §3.1.8) is augmented to include

35 pp-number:

pp-number p sign
pp-number P sign

Example

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<float.h> for an IEEE 754 implementation might contain:

#define FLT_MAX 0x1.FFFFFEp127f /* or 0xF.FFFFFp124f */

#define FLT_EPSILON 0x1p-23f

#define FLT_MIN 0x1p-126f

Example

The constant -0x1.0000000000000p0 represents the largest IEEE 754 double precision value less than -1.

Hexadecimal more clearly expresses the significance of floating constants.

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The binary-exponent part is required to avoid ambiguity from an f suffix (being mistaken as a hexadecimal digit).

Constants of long double type are not generally portable, even among IEEE implementations.

Unlike integers, floating values cannot all be represented directly by hexadecimal constant syntax. A sign can be prefixed for negative numbers and -0. Infinities might be produced by hexadecimal constants that overflow. NaNs require some other mechanism. Note that 0x1.FFFFFEp128f, which might appear to be an IEEE single-format NaN, in fact overflows to an infinity in the single format (and causes a translation-time warning).

Infinity and NaN constants, useful for static and aggregate initialization, should be considered for future extensions.

An alternate approach might have been to represent bit patterns. For example

#define FLT_MAX 0x.7F7FFFFF

This would have allowed representation of NaNs and infinities. However, numerical values would have been more obscure owing to bias in the exponent and the implicit significand bit. NaN representations would not have been portable—even the determination of IEEE quiet NaN vs signaling NaN is implementation-defined. NaNs and infinities are provided through macros in §4.3.

The straightforward approach of denoting octal constants by a 0 prefix would have been inconsistent with allowing a leading 0 digit—a moot point as the need for octal floating constants was deemed insufficient.

The caret ^ was ruled out as a character to introduce the exponent because doing so would have used up a potential operator.

3.2 Conversions

3.2.1 Floating and integral (ISO §6.2.1.3; ANSI §3.2.1.3)

For conversion from floating to integer type, if the floating value is infinite or NaN or if the integral part of the floating value exceeds the range of the integer type then the invalid exception, if available, is raised and the value of the result is unspecified.

For IEEE Implementations

Whether conversion of nonintegral floating values whose integral part is within the range of the integer type raises the inexact exception is unspecified.

Conversion from floating to integral rounds toward zero, consistent with Standard C. IEEE rounding is provided by the library function rinttol.

IEEE standard 854, though not 754, directly specifies that floating-to-integral conversion raise the inexact exception for nonintegral in-range values. In those cases where it matters, library functions can be used to effect such conversions with or without raising the inexact exception. See rint, rinttol, and nearby int in §F.6.

Conversion from integer to floating type is an IEEE standard floating-point operation, rounding according to the current rounding direction mode.

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Note that rounding indeed will be required if an integer is too wide to represent exactly in the floating-point format.

5 3.2.2 Floating types (ISO §6.2.1.4; ANSI §3.2.1.4)

For IEEE Implementations

Conversions between floating types are specified by the IEEE floating-point standards.

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3.2.3 Expression evaluation (ISO §6.2.1.5; ANSI §3.2.1.5)

This specification recognizes five distinct expression evaluation methods. A floating-point expression has both a semantic type and an evaluation format. Each evaluation format is the format of one of the floating types. The result of the expression is represented in the expression's evaluation format. An expression evaluation method determines the evaluation formats for expressions. Which expression evaluation methods are provided is implementation-defined.

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For most floating operations Standard C defines the semantic type of the operation to be the widest type of its operands, but gives explicit license to represent the operation's result in a format wider than its type.

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The use here of the term method is unrelated to its use in Smalltalk.

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Although specifying just one method would have facilitated porting code, any one method would have been unacceptably inefficient on some important architectures. On the other hand, still other expression evaluation methods are conceivable, for example evaluating float operations to float format, and all others to long double. The expression evaluation methods described in this section comprise an intentionally small set with at least one method that is efficient for any of the existing or anticipated, commercially significant, floating-point architectures:

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Floating-point architectures

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In the following description of floating-point architectures, the terms extended, double, and single have a slightly broader meaning than in the rest of this document. They still refer to floating formats, but apply to both IEEE and non-IEEE systems. Generally, extended is wider than double which is wider than single.

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Extended-based. The arithmetic engine is extended. Source operands can be single, double, or extended, though generally arithmetic with single and double types is less efficient, requiring extra conversions. Examples include Intel 80x87, Cyrix 3D87, Motorola 6888x, and AT&T WE 32x06. The Motorola 88110 and Intel 960 can be used as extended-based architectures, or alternatively as single/double/extended ones (see below).

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Double-based. The arithmetic engine is double. Source operands can be single or double, though generally arithmetic with the single type is less efficient, requiring extra conversions. Extended may be available, but implemented in software. Examples include IBM RISC System/6000, PDP-11 in double mode, CRAY, and CYBER 180. On CRAY and CYBER, single and double may be the same format. The CYBER provides some hardware support for extended.

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Single/double. These provide orthogonal operations for single and double arithmetic. Single is typically faster than double. Extended may be available, but implemented in

software. Examples include MIPS, SPARC, HP PA-RISC, Motorola 88100, Intel 860, and systems assembled with Weitek or BIT processors. The MIPS, SPARC, and HP PA-RISC architectures specify extended, though it is not yet in hardware.

Single/double/extended. These provide orthogonal operations for single, double, and extended arithmetic. Single is faster than double, which is faster than extended. Examples include Motorola 88110, Intel 960, IBM S/370, and VAX.

3.2.3.1 Methods

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The expression evaluation methods are characterized by two properties: (1) the minimum-width format (float, double or long double) for expression evaluation, and (2) whether determination of the evaluation format is affected by the context of the operation according to the rules for widest-need evaluation (explained below). The combinations of these two properties yield the five expression evaluation methods:

	min-eval-format	widest-need
1.	float	no
2.	double	no
3.	long double	<irrelevant></irrelevant>
4.	float	yes
5.	double	yes

Minimum evaluation format. The minimum evaluation format may be float, double, or long double. The evaluation format for operations subject to the usual arithmetic conversions and for floating constants is at least this wide, even if the semantic type is less.

The early C implementations provided just the float and double floating-point types and evaluated all floating expressions to double. Intentional or not, some C programs have relied on extra precision for their computation with float operands. A minimum evaluation format of double is a natural choice for double-based architectures.

Implementations for single/double and single/double/extended architectures may find a minimum evaluation format of float compellingly more efficient, despite potential problems of conformity to expectations based on C's tradition of wide evaluation.

Even on a single/double or single/double/extended architecture, an implementation might provide double as a minimum evaluation format, for compatibility reasons. Common statements of the form

```
f1 = f2 op f3; /* where f1, f2, f3 are of type float */
```

can be done optimally by many such implementations, including all IEEE ones, where rounding the result to double and then to float is equivalent to rounding to float directly.

A minimum evaluation format of long double is common on extended-based architectures. Programs that run under one of the other expression evaluation methods generally run at least as well when all expressions are evaluated to long double. Most program failures due to extra precision arise from its inconsistent use (see §B.5).

Representation of constants in a format commensurate with expression evaluation, not a traditional practice, better meets certain expectations than would representation strictly according to semantic type—for example, 0.1f == 1.0f/10.0f. Viewed as translation-

time operations that convert decimal strings to internal floating representations, literal floating constants naturally follow the method of expression evaluation.

Without widest-need evaluation. Without widest-need, the evaluation format for an operation or constant is simply the wider of its semantic type and the minimum evaluation format.

With widest-need evaluation. With widest-need, the evaluation format for an operation is the widest of the semantic types appearing in a certain enclosing expression and at least as wide as the minimum evaluation format. More precisely, the evaluation format for an operation subject to the usual arithmetic conversions, or for an assignment (including the assignment of function arguments to parameters, but not cast conversions), is propagated to its operands (or arguments): if an operand is a variable or an operation not subject to the usual arithmetic conversions it is converted to the evaluation format; if the operand is an operation subject to the usual arithmetic conversions, or a floating constant, the evaluation format is imposed recursively.

Examples

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With the declarations

float f;
double d;
long double ld;
double dd(double);
double fd(float);

widest-need with a minimum evaluation format of float implies:

30	Outer-most expression	Operation	Evaluation format
	ld + (f * f)	in læphesne	long double
		ancings writing	long double
35	ld + fd(f * f)	*	float
		+	long double
	ld + dd(f * f)	omic aperada	double
40		oringo \$ 65 ca	long double
40	ld + (d = f * f)		double
	ther contraction operators are		long double
	f + (d = 1d * 1d)	*	long double
45		+	double
	ld + (double)(f * f)	giga ard districtly (1977) Annote skyle Southernoon	float
		+	long double
50	ld + (d -= f * f)	*	double
		_	double
		+	long double
	ld + (f++ *d)	++	float
55			double
		*	long double
		+	long double
	ld == f * f	*	long double

	f / (d + d, f * f)		double float float
5	f + (f - f ? d / d : ld)	# 10 To 10	float long double long double
10	ld + 0.1f	0.1f +	long double
	f + 0.1 7 10 200 ETSVED		double double
15			banusug angal i

The definition of widest-need is based on a widest need evaluation for Fortran presented in [9]. It does not affect integer expression evaluation, which is covered by Standard C.

As computer speed and memory size increase, so will the number of problems attempted and the size of data sets. Thus, the likelihood that a program will suffer serious roundoff error for some actual data will increase. Wider precision, not for the entire computation but just for expressions containing certain variables, often will fix the problem, without unduly affecting performance, and without requiring costly error analysis. With widest-need, an expression is automatically evaluated to the format of its widest component. To achieve the same effect without widest-need expression evaluation, the programmer must add or delete casts and constant suffixes throughout the program.

Widest-need expression evaluation is a particularly attractive compromise for architectures whose wider formats are significantly slower. It offers the accuracy of wide evaluation where likely needed and also the speed of narrow evaluation where clearly intended. Note that casts can be used to inhibit widest-need widening, even within a wide expression.

Previous drafts defined a *pragma evaluate which allowed switching expression evaluation methods between external declarations. This facility was believed to be without sufficient utility and somewhat error prone. Implementations that support multiple expression evaluation methods can supply translation options.

3.2.3.2 Contraction operators

A floating-point engine may provide an atomic operation for multiple binary operators. Such an atomic operation is referred to here as a contraction operator and the multiple binary operators as contracted, because rounding errors or side effects from their computation may be omitted. Contracted operators should incur no greater-magnitude rounding error than if they were not contracted. Whether contraction operators are employed is implementation-defined.

An implementation that is able to multiply two double operands and produce a float result in just one machine instruction might contract the multiplication and assignment in:

```
float f;
double d1, d2;
...
f = d1 * d2;
```

Other examples of potential contraction operators include:

```
compound assignments +=, -=, etc.;
ternary add x + y + z;
multiply-add x * y + z.
```

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Contractions can lead to subtle anomalies even while increasing accuracy. The value of expressions like a * b + c * d will depend on how the translator uses a contracted multiply-add. Knowing that the implementation contracts multiply-adds, the programmer should be able to control results (and reap the benefits of contraction) through simple coding measures, for example parenthesizing (a * b) + c * d. However, the Intel 860's multiply-add is slightly more problematic. Since it keeps a wide but partial product, a * b + z may differ from c * d + z even though the exact mathematical products a * b and c * d are equal; the result depends not just on the mathematical result and the format, as ordinarily expected for error analysis, but also on the particular values of the operands.

The extra accuracy of the IBM RISC System/6000's fused multiply-add, which produces a result with just one rounding, can be exploited for simpler and faster codes. See [19] for details.

The fp_contract pragma can be used to allow or disallow contraction operators.

#pragma fp_contract on-off-switch

This pragma can occur outside external declarations, and allows or disallows contraction operators from its occurrence until another fp_contract pragma is encountered, or until the end of the translation unit. The default state (on or off) for the pragma is implementation-defined.

25 For IEEE Implementations

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Contraction operators honor infinities, NaNs, signed zeros, subnormals, and the rounding directions in a manner consistent with the basic arithmetic operations covered by the IEEE floating-point standards. Contraction operators should raise exceptions in a manner generally consistent with the basic arithmetic operations covered by the IEEE floating-point standards.

Contraction operators should deliver the same value as their uncontracted counterpart, else be correctly rounded—that is, deliver the infinitely precise result of their contracted operations, rounded (once) to the destination format according to the effective rounding method.

3.2.4 Wide representation

Three pragmas give license for the implementation to represent function return values, function parameters, and variables in a format wider than their declared type.

```
#pragma fp_wide_function_returns on-off-switch
#pragma fp_wide_function_parameters on-off-switch
#pragma fp_wide_variables on-off-switch
```

#pragma fp_wide_function_returns on—allows floating return values to be represented in a wider format than (and not narrowed to) the declared type of the function.

*pragma fp_wide_function_parameters on—allows floating parameters to be in a wider format than (and not narrowed to) the declared type of the formal parameter.

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#pragma fp_wide_variables on—allows values of automatic scalar floating variables to be in a wider format than their declared type.

If the *on-off-switch* is off then widening is disallowed. The default state for these pragmas is off.

Standard C compatibility requires that the default state for the pragmas be off.

These pragmas can occur outside external declarations, and allow (if on) or disallow (if off) widening from their occurrence until another pragma instructing otherwise is encountered, or until the end of the translation unit. The effect of these pragmas appearing inside an external declaration is undefined. Widening is consistent throughout the effect of an enabling pragma: either all instances of the returns, parameters, or variables are widened or none are; the representation format for a parameter or variable does not vary. However, which, if any, of these pragmas actually cause widening is implementation-defined. The fp_wide_function_returns and fp_wide_function_parameters pragmas may affect function definitions or calls but not prototypes.

When the implementation detects an address or sizeof operator of a widened parameter or variable it emits a translation-time warning; execution-time behavior is then undefined.

This mechanism facilitates generating efficient code for extended-based or double-based architectures. §3.2.3 and §4.3 provide rationale. The typedefs float_t and double_t allow finer application than do the pragmas, but require more extensive changes to existing code.

The function writer who decides that narrowing arguments and returns to their semantic type is less desirable than efficiency can write the function under the effect of enabling fp_wide_function_parameters and fp_wide_function_returns pragmas. Similarly the programmer who uses the function can apply these pragmas to the call site. In either case widening (not narrowing) may or may not occur. These pragmas do not demand widening, nor even recommend it, but merely declare that widening would be acceptable. It is up to the implementation to determine whether widening would be both safe and also more efficient. For example, implementations that pass different type (floating) parameters in different formats can not widen parameters of external functions safely.

Even among implementations which respond to the pragmas, the location in the source code where the pragmas must be placed to be effective may vary. For example, an implementation might perform requisite narrowing of parameters at the call site, in which case the call would have to be under the effect of an enabling fp_wide_function_parameters pragma; or, it might narrow within the function, in which case the function definition would have to be under the effect of the pragma.

The pragmas do not affect function prototypes. Doing so might have benefited implementations that pass different floating type arguments and returns in different ways. However, maintaining consistency between the prototype and implementation seemed particularly error prone. A language extension to assure the consistency seemed unjustified. The float_t and double_t type definitions are available for such prototypes.

Casts are not affected by any of these pragmas, nor by wide expression evaluation, so can be used portably to force narrowing.

Another approach would have been to introduce register as a function qualifier that would have allowed widening of both the parameters and the return value. This would have been

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inconsistent with the register storage class specifier, which is unrelated to widening, and would not have helped with variables.

3.3 Expressions (ISO §6.3; ANSI §3.3)

3.3.1 The arithmetic operators (ISO §6.3.3.1, 6.3.3.3, 6.3.4-6.3.6, 6.3.16; ANSI §3.3.3.1, 3.3.3.3, 3.3.4-3.3.6, 3.3.16)

The implementation should follow the guide referenced in Appendix E to document its arithmetic operators.

For IEEE Implementations

These operations fall under the specification of the IEEE floating-point standards:

++ -- + - * / = casts += -= *= /=

The IEEE floating-point standards require that, given default rounding precision, these operations be rounded to the precision of their evaluation format.

3.3.2 Relational and equality operators (ISO §6.1.5, 6.3.8, 6.3.9; ANSI §3.1.5, 3.3.8, 3.3.9)

The Standard C relational and equality operators support the usual mathematical relationships between numeric values. These operators are augmented to support relationships involving nonnumeric values, NaNs. For any ordered pair of numeric values exactly one of the relationships—less, greater, and equal—is true. For a NaN and a numeric value, or for two NaNs, just the unordered relationship is true.

Symbol Relation less < greater less or equal <= 35 greater or equal >= equal unordered, less, or greater unordered !<>= less or greater <> 40 less, equal, or greater unordered or greater !<= unordered, greater, or equal ! < unordered or less !>= unordered, less, or equal !> unordered or equal 45

The additional operators are analogous to, and have the same precedence as, the Standard C relational operators. Where the operands have types and values suitable for relational operators, the semantics detailed in ISO §6.3.8 (ANSI §3.3.8) apply.

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The Standard C operator syntax (ISO §6.1.5; ANSI §3.1.5) is augmented to include the additional operators.

Programs written for (or ported to) systems with NaNs will be expected to handle invalid and NaN input in reasonable ways. The additional relational operators support such programs. As operators they, together with the arithmetic operators (+, *, ...), provide a consistent approach to handling NaNs: the arithmetic operators simply propagate them; the relational operators facilitate directing them through branches. Thus NaNs can flow through many computations without the need for obfuscating or inefficient code.

The alternative of function syntax, such as

```
isrelation(x, FP_UNORDERED | FP_LESS | FP_EQUAL, y)
```

instead of x !> y, would not have required language extensions, and could have been as efficient as built-in operators, though only if the functions were built into the translator. However, special function calls for comparisons would have been arguably more awkward and inconsistent with the overall approach to NaNs.

The set of relational operators is obtained by allowing the > combinations and extending the notion of negated operators, previously only !=, to the relational operators, !<, etc.

The expressions (a !op b) and ! (a op b) always have the same logical value, that is (a !op b) == ! (a op b), where op is <, >, <=, >=, <>, or <>=. But if the types of a and b admit NaNs, then ! (a op b) and (a !op b) may differ in their exception behavior. Implementations without NaNs, and non-IEEE implementations with NaNs but which practically cannot support the specification below for IEEE implementations, can regard the new relationals simply as notational alternatives.

In its definitions for the logical AND, logical OR, and conditional operators and the if statement, Standard C assumes that any expression compares equal to 0 if and only if it does not compare unequal to 0. This assumption is still valid: a == 0 is true if and only if a == 0 is false, even if a is a NaN.

The implementation should follow the guide referenced in Appendix E to document its relational and equality operators.

For IEEE Implementations

For just those relational operators that include < or > but not !, the invalid exception is raised if the operands compare unordered.

For example,

$$(a < b) == !(a ! < b)$$

in all cases, but (a < b) raises invalid when a and b compare unordered whereas !(a !< b) does not.

The somewhat awkward articulation !(a !< b) for a non-exceptional less than is a consequence of the IEEE floating-point standards' priority on supporting existing code that does not account for NaNs. When x or y is a NaN, any value for x < y, whether the actual result 0 (false) or its alternative 1 (true), is likely to be misleading; so the IEEE standards require that such tests raise the invalid exception. Tests of equality give generally useful results when operands are NaNs, hence do not raise the invalid exception.

The IEEE floating-point standards enumerate 26 functionally distinct comparison predicates, from combinations of the four comparison results and whether invalid is raised. Use of

logical negation extends the 14 relational and equality operators listed above to the full 26. (There are 26 not 28 because == and != never raise invalid).

This proposal supplants a previous one which would have augmented the set of relations by using the ? symbol to denote unordered, for example a ?>= b instead of a !< b. Use of the ? relationals would have had the advantage that the unordered case would have been dealt with explicitly. However, the ! relationals are a more natural language extension, particularly from the point of view of programmers for (non-IEEE) implementations not detecting unordered. Also, using ?? as proposed for the unordered operator would have conflicted with Standard C trigraphs.

Without any language or library support a !> b might be implemented by

a != a || b != b || a <= b

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However, even more awkward code would be required if a or b had side effects. The programmer would have to remember to put the NaN tests first, and trust the compiler not to replace a != a || b != b by false. Also, special optimization would be necessary to generate efficient code. Use of functions like isnan or isunordered, which are recommended in the appendixes to the IEEE floating-point standards, is similarly problematic.

3.4 Constant Expressions (ISO §6.4; ANSI §3.4)

A constant expression, other than one in an initializer for an object that has static storage duration or in an initializer list for an object that has aggregate or union type, is evaluated (as if) during execution.

This is merely a clarification of Standard C. See §B.4 regarding optimization.

30 Example

For the aggregate and static initializations, the division is done at translation time, raising no (execution-time) exceptions. On the other hand, for the two automatic scalar initializations the invalid division occurs at execution time.

Previous versions of this section allowed translation-time constant arithmetic, but empowered the unary + operator, when applied to an operand, to inhibit translation-time evaluation of constant expressions. The programmer can achieve the efficiency of translation-time evaluation by using static initialization, for example

```
static double one_third = 1.0/3.0;
```

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or to decrease the likelihood of storage allocation

```
const static double one_third = 1.0/3.0;
```

For IEEE Implementations

This specification acknowledges the semantics of IEEE arithmetic for the as if principle. In particular, execution-time operations must be affected by modes and must raise exceptions as required by the IEEE floating-point standards.

Note that results of inexact expressions like 1.0/3.0 can be affected by rounding modes set at execution time, and expressions such as 0.0/0.0 and 1.0/0.0 can be used reliably to generate execution-time exceptions.

3.5 Initialization (ISO §5.1.2, 6.5.7; ANSI §2.1.2, 3.5.7)

All computation for automatic scalar initialization is done (as if) at execution time. All computation for initialization of objects that have static storage duration or that have aggregate or union type is done (as if) at translation time.

Standard C does not specify when aggregate and union initialization is done. Otherwise, this is merely a clarification of Standard C. Note that, under the effect of an enabling fenv_access pragma, any exception resulting from execution-time initialization must be raised at execution time. See §B.4 regarding optimization.

Example

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```
#pragma fenv_access on
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       void f(void) {
          float u[] = { 1.1e75 };
                                        /* does not raise exceptions */
          static float v = 1.1e75;
                                        /* does not raise exceptions */
          float w = 1.1e75;
                                        /* may raise exceptions */
          double x = 1.1e75;
                                        /* may raise exceptions */
30
          float y = 1.1e75f;
                                        /* may raise exceptions */
          long double z = 1.1e75;
                                        /* does not raise exceptions */
```

The aggregate and static initializations of u and v raise no (execution-time) exceptions because their computation is done at translation time. The automatic initialization of w requires an execution-time conversion to float of the wider value 1.1e75, which raises exceptions on some implementations, including all IEEE ones. The automatic initializations of x and y entail execution-time assignment, but, in some expression evaluation methods, not to a narrower format, in which case no exceptions need be raised. The automatic initialization of z entails execution-time assignment, but not to a narrower format, so no exception is raised. Note that the conversions of the floating constants 1.1e75 and 1.1e75f to their internal representations occur at translation time in all cases.

Use of float_t and double_t variables increases the likelihood of translation-time computation. For example, the automatic initialization

```
double_t x = 1.1e75;
```

could be done at translation time, regardless of the expression evaluation method.

The specification of §3.4-5 does not suit C++, whose static and aggregate initializers need not be constant. Specifying all floating-point constant arithmetic and initialization to be (as if) at execution time would be consistent with C++ and, given the fenv_access mechanism, still would allow the bulk of constant arithmetic to be done, in actuality, at translation time.

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For IEEE Implementations

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This specification acknowledges the semantics of IEEE arithmetic for the as if principle.

In particular, execution-time operations must be affected by modes and must raise exceptions as required by the IEEE floating-point standards.

3.6 Predefined Macro Names (ISO §6.8.8; ANSI §3.8.8)

10	FPCE	The decimal constant 1, indicating conformance to this specification.			
	FPCE_IEEE	The decimal constant 1, indicating conformance to the parts of this specification for IEEE implementations.			

4. LIBRARY

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4.1 Introduction (ISO §7.1.2, 7.1.6; ANSI §4.1.2, 4.1.6)

Section 4.2 covers numerical extensions to the Standard C libraries. Section 4.3 documents a new header <fp.h> which provides facilities for general floating-point programming; <fp.h> supersedes <math.h>. Section 4.4 documents a new header <fenv.h> which provides access to the floating-point environment. The identifiers with external linkage declared in either <fp.h> or <fenv.h> are reserved for use as identifiers with external linkage only if at least one inclusion of either <fp.h> or <fenv.h> occurs in one or more of the translation units that constitute the program. In other regards, <fp.h> and <fenv.h> follow the Standard C specification for standard headers and reserved identifiers (ISO §7.1.2, 7.1.2.1; ANSI §4.1.2, 4.1.2.1).

This specification for new identifiers with external linkage follows that in [25].

In some cases names are not unique in the first six characters, unlike in Standard C.

4.2 Standard C Library Extensions

4.2.1 General utilities <stdlib.h>

4.2.1.1 The atof function (ISO §7.10.1.1; ANSI §4.10.1.1)

#include <stdlib.h>
double atof(const char *nptr);

The atof function meets the specifications below for strtod.

This document does not require float and long double versions of atof, but instead encourages the use of strtof and strtold which have a more generally useful interface.

4.2.1.2 The strtof, strtod, and strtold functions (ISO §7.10.1.4; ANSI §4.10.1.4)

#include <stdlib.h>
double strtod(const char *nptr, char **endptr);
float strtof(const char *nptr, char **endptr);
long double strtold(const char *nptr, char **endptr);

The strtof and strtold functions are float and long double versions of strtod. Their behavior is the same as that of strtod. However, if the correct value is outside the range of representable values, strtof and strtold return HUGE_VALF and HUGE_VALL, respectively, with the appropriate sign. (HUGE_VALF and HUGE_VALL are introduced in §4.3.)

Translation-time conversion of valid floating constants exactly matches execution-time conversion provided the default rounding modes are in effect. See §3.1.2.

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The expected form of the subject sequence accepted by strtod is broadened to include an optional plus or minus sign, then a 0x or 0x, and then followed by one of:

- 1. a nonempty sequence of hexadecimal digits optionally containing a "decimal-point" character, then a binary-exponent part, but no floating suffix;
- 2. a nonempty sequence of hexadecimal digits containing a "decimal-point" character, but no floating suffix.
- For implementations whose FLT_RADIX is a power of 2, a hexadecimal floating source value is correctly rounded to the appropriate internal format. For implementations whose FLT_RADIX is not a power of 2, the result should be one of the two numbers in the appropriate internal format that are adjacent to the hexadecimal floating source value, with the extra stipulation that the error have the correct sign for the current rounding direction.

Also, the syntax accepted by strtod includes:

sign_{Opt} inf
20 sign_{Opt} infinity
sign_{Opt} nan
sign_{Opt} nan(n-char-sequence_{Opt})

where

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n-char-sequence:
digit
nondigit
n-char-sequence digit
n-char-sequence nondigit

and any strings equivalent except for case in the INF, INFINITY, or NAN part.

The character sequences INF and INFINITY produce an infinity, if representable, else are treated as numeric input that overflows.

Character sequences of the form NAN or NAN (*n-char-sequence_{Opt}*) are converted to quiet NaNs, if supported, else are treated as invalid input. An implementation may use the *n-char-sequence* to determine extra information to be represented in the NaN's significand; which *n-char-sequence*'s are meaningful is implementation-defined.

So much is implementation-defined because so little is portable. Attaching meaning to NaN significands is problematic, even for one implementation, even an IEEE one. For example, the IEEE floating-point standards do not specify the effect of format conversions on NaN significands—conversions, perhaps generated by the compiler, may alter NaN significands in obscure ways.

Requiring a sign for NaN or infinity input was considered as a way of minimizing the chance of mistakenly accepting nonnumeric input. The need for this was deemed insufficient, partly on the basis of prior art.

For simplicity, the infinity and NaN representations are provided through straightforward extensions, rather than through a new locale (ISO §7.4; ANSI §4.4). Note also that Standard C locale categories do not affect the representations of infinities and NaNs.

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The strtod function should honor the sign of zero if the arithmetic supports signed zeros.

5 For IEEE Implementations

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Conversion from a numeric decimal string with DECIMAL_DIG (defined in §4.3) or fewer significant digits to the widest supported IEEE format is correctly rounded according to the effective rounding direction. For conversion of a numeric decimal string D, with more than DECIMAL_DIG digits, consider the two bounding, adjacent decimal strings L and U, both having DECIMAL_DIG significant digits, such that the values of L, D, and U satisfy $L \le D \le U$. The result of conversion is one of the (equal or adjacent) values that would be obtained by correctly rounding L and U according to the current rounding direction, with the extra stipulation that the error with respect to D has the correct sign for the current rounding direction.

Correct rounding refers to the style of rounding that the IEEE floating-point standards prescribe for their arithmetic operations: the delivered value is the (destination) format's value that is closest, in the sense of the effective rounding direction, to the infinitely precise result.

DECIMAL_DIG is sufficiently large that L and U will usually round to the same internal floating value, but if not will round to adjacent values.

The IEEE floating-point standards require perfect rounding for a large though incomplete subset of decimal conversions. This specification goes beyond the IEEE floating-point standards by requiring perfect rounding for all decimal conversions, involving DECIMAL_DIG or fewer decimal digits and a supported IEEE format, because practical methods are becoming publicly available (see [12]). Although not requiring correct rounding for arbitrarily wide decimal numbers, this specification is sufficient in the sense that it ensures that every internal numeric value in an IEEE format can be determined as a decimal constant.

The strtod function honors the sign of zero. It treats the overflow, underflow, and inexact exceptions in accordance with the IEEE floating-point standards. And, it raises the invalid exception on invalid numeric input.

This document's previous specification that strtod return a NaN for invalid numeric input, as recommended by IEEE standard 854, was withdrawn because of the incompatibility with Standard C, which demands that strtod return 0 for invalid numeric input.

4.2.2 Input / output <stdio.h>

4.2.2.1 The fprintf function (ISO §7.9.6.1; ANSI §4.9.6.1)

The a and a conversion specifiers provide hexadecimal floating representations. The conversion specifier a means that the argument is converted to a hexadecimal floating representation in the style [-]0xh.hhhhptd. The number of hexadecimal digits h after the decimal-point character is equal to the precision; if the precision is missing then for implementations whose FLT_RADIX is a power of 2 the precision is sufficient for an exact representation of the source value, and for other implementations the precision should be sufficient to distinguish (see rationale below) values of the source type, except that trailing zeros may be omitted. The hexadecimal digit to the left of the decimal-point character is nonzero for normal values and is otherwise chosen by the

implementation; if the precision is zero and the # flag is not specified, no decimal-point character appears. The a conversion specifier will produce a number with x and P instead of x and p. The exponent always contains at least one digit, and only as many more digits as necessary to represent the decimal exponent of 2. Binary implementations should choose the hexadecimal digit to the left of the decimal-point character so that subsequent digits align to nibble boundaries. For example, the next value greater than one in the common IEEE 754 80-bit extended format should be 0x8.00000000000001p-3 The next value less than one in IEEE 754 double should be 0x1.fffffffffffp-1 Note that if the precision is missing, trailing zeros may be omitted. For example, the value positive zero might be 0 + q.0x0The more suggestive conversion specifiers for hexadecimal formatting, namely x and h, were unavailable. Since h was taken H was ruled out in favor of a lower/upper case option. Possibilities other than a included: b j k m q r t v w y z. The optional h to indicate hexadecimal floating, as in the, was deemed a less natural fit with the established scheme for specifiers and options. The decimal-point character is defined in Standard C (ISO §7.1.1; ANSI §4.1.1). Radixpoint character would have been a better term. The precision p is sufficient to distinguish values of the source type if where b is FLT_RADIX and n is the number of base-b digits in the significand of the source type. A smaller p might suffice depending on the implementation's scheme for determining the digit to the left of the decimal-point character. (See [6], Ch 7.) For implementations whose FLT_RADIX is a power of 2, the source value is correctly rounded to a hexadecimal floating number with the given precision. implementations whose FLT_RADIX is not a power of 2, the result should be one of the two adjacent numbers in hexadecimal floating style with the given precision, with the extra stipulation that the error have the correct sign for the current rounding direction.

two adjacent numbers in nexadecimal floating style with the given precision, with the extra stipulation that the error have the correct sign for the current rounding direction.

The F conversion specifier has the same effect as f except for infinity and NaN formatting (specified below).

The optional precision, optional L, and 0 and # flag characters all have the same effect for a, A, and F conversions as for e, E, f, g, and G.

With e-style formatting, the exponent field contains at least two digits, and only as many more digits as necessary to represent the exponent.

For all floating conversions, an infinite value is converted in one of the styles [-] inf or [-] infinity—which style is implementation-defined.

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For all floating conversions, a NaN value is converted in one of the styles [-]nan or [-]nan (n-char-sequence)—which style, and the meaning of any n-char-sequence, is implementation-defined.

See §4.2.1.2 Rationale.

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When applied to infinite and NaN values, the -, +, and space flag characters have their usual meaning; the # and 0 flag characters have no effect.

Use of an upper case format specifier, A, E, F, or G, results in INF, INFINITY, or NAN instead of inf, infinity, or nan.

Use of the A and F format specifiers constitutes a minor extension to Standard C which does not reserve them.

The results of all floating conversions of a negative zero should include a minus sign.

For IEEE Implementations

- If the number of significant decimal digits is at most DECIMAL_DIG, then the result from converting a value from an IEEE format is correctly rounded for the current rounding direction. If the number of significant decimal digits is more than DECIMAL_DIG but the source value is exactly representable with DECIMAL_DIG digits, then the result is an exact representation with trailing zeros. Otherwise, the source value is bounded by two adjacent decimal strings L < U, both having DECIMAL_DIG significant digits; the value of the result decimal string D satisfies L ≤ D ≤ U, with the extra stipulation that the error have the correct sign for the current rounding direction.
- See §4.2.1.2 Rationale. For binary-to-decimal conversion, the *infinitely precise result* is just the source value, and the destination format's values are the numbers representable with the given format specifier. The number of significant digits is determined by the format specifier, and in the case of fixed-point conversion by the source value as well.
 - The results of all floating conversions of a negative zero shall include a minus sign.

4.2.2.2 The fscanf function (ISO §7.9.6.2; ANSI §4.9.6.2)

For a, A, e, E, f, F, g, and G conversion specifiers, all valid syntax—including hexadecimal-floating-constant, infinity, NaN, and signed zero—is treated in the same manner as strtod.

4.3 Floating-Point Extensions <fp.h>

The header <fp.h> declares several types, macros and functions to support general floating-point programming. It provides essentially all of Standard C <math.h>, as well as facilities required or recommended by the IEEE floating-point standards, and a few other facilities that have proved broadly useful. [17] and [1] contain basic descriptions, not repeated in this document, of the Standard C functions. Appendix F contains specification that is particularly suited for IEEE implementations. The implementation should follow the guide referenced in Appendix E to document its <fp.h> functions.

The typedefs

float_t
double_t

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are defined to be the implementation's most efficient floating types at least as wide as float and double, respectively. (Every value of type float_t is also a value of type double_t.)

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Facility to use wider types is needed for writing portable efficient code. Currently Standard C gives no way of asking for the most efficient floating type with at least a given width. Thus different prototypes are more efficient on different floating-point architectures.

15	architecture (see §3.2.3)	most efficient prototype	
	extended-based	long double f(long double)	
	double-based	double f(double)	
	single/double	float f(float)	
	single/double/extended	float f(float)	

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Differences may involve whether values can be kept in registers, hence are substantial. Implementations for the various floating-point architectures might use these type definitions:

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4	øq	J	•	

architecture	float_t	double_t	
extended-based	long double	long double	
double-based	double	double	
single/double	float	double	
single/double/extended	float	double	

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An alternate approach of modifying the semantics of the register storage-class specifier, when applied to a floating type, to mean that the associated value may be wider than the type, was rejected as inconsistent with existing use of register in Standard C.

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The macro

HUGE_VAL

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is as defined in ANSI C §4.5.

The macros

HUGE_VALF HUGE_VALL

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are float and long double analogs of HUGE_VAL. They expand to positive float and long double expressions, respectively. Like HUGE_VAL, each can be a positive infinity in an implementation that supports infinities.

The macro

INFINITY

expands to a floating expression representing an implementation-defined positive or unsigned infinity, if available, else to a positive floating constant that overflows at translation time.

The macro

NAN

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is defined if and only if the implementation supports quiet NaNs. It expands to a floating-point expression representing an implementation-defined quiet NaN.

Ideally the INFINITY and NAN macros would be suitable for static and aggregate initialization, though currently such is not required by this specification.

No type is specified for the INFINITY and NAN macros because conversions between floating-point types convert infinities to infinities and NaNs to NaNs, without raising exceptions.

The macros

25 FP_NAN

FP_INFINITE

FP_NORMAL

FP_SUBNORMAL

FP_ZERO

are for number classification. They represent the mutually exclusive kinds of floating-point values. They expand to int constant expressions with distinct values and suitable for use in #if preprocessing directives.

Some prior art uses a finer classification: FP_POS_INFINITE, FP_NEG_INFINITE, etc. The current consensus is that those specified, in conjunction with the signbit macro, are generally preferable.

Results for the inquiry macros specified in the remainder of this section are undefined if the argument is not of floating type.

This allows efficient implementation.

The macro

fpclassify(floating-expr)

evaluates to the value of the number classification macro appropriate to the value of its argument. First, an argument represented in a format wider than its semantic type is converted to its semantic type. Then classification is based on the type of the argument.

It is important to know the type that classification is based on. For example, a value might be zero when converted to float, subnormal when converted to double, and normal when converted to long double.

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fpclassify might be implemented as

#define fpclassify(x) ((sizeof(x) == sizeof(float)) ? __fpclassifyf(x) \
 : (sizeof(x) == sizeof(double)) ? __fpclassifyd(x) \
 : __fpclassifyl(x))

The macro

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signbit(floating-expr)

evaluates to an int expression that is nonzero if and only if the sign of the argument (infinities, zeros, and NaNs included) is negative.

The IEEE floating-point standards do not specify the effect of arithmetic operations on a NaN's sign bit. However, signbit of a NaN is valid in the sense that, even if x is a NaN, signbit (x) is invariant until x changes.

The macro

20 isfinite(floating-expr)

evaluates to an int expression that is nonzero if and only if its argument has a finite value (zero, subnormal, or normal). First, an argument represented in a format wider than its semantic type is converted to its semantic type. Then determination is based on the type of the argument.

The macro

isnormal(floating-expr)

evaluates to an int expression that is nonzero if and only if its argument value is normal: neither zero, subnormal, infinite, nor NaN. First, an argument represented in a format wider than its semantic type is converted to its semantic type. Then determination is based on the type of the argument.

The macro

isnan(floating-expr)

evaluates to an int expression that is nonzero if and only if its argument value is a NaN.

The macro

45 DECIMAL DIG

expands to an int constant expression suitable for use in #if preprocessing directives. Its value is an implementation-defined number of decimal digits which is supported by conversion between decimal and all internal floating-point formats. Conversion from (at least) double to decimal with DECIMAL_DIG digits and back should be the identity function. And, DECIMAL_DIG should give an appropriate number of digits to carry in canonical decimal representations.

In order that correctly rounded conversion from an internal floating-point format with precision m to decimal with DECIMAL_DIG digits and back be the identity function, DECIMAL_DIG should be a positive integer n satisfying

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 $10^{n-1} > \text{FLT}_{\text{RADIX}}^{m}$,

if FLT_RADIX is 10 otherwise

Refer to [6], Chapter 7, for details.

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DECIMAL_DIG is distinct from Standard C's DBL_DIG, which is defined in terms of conversion from decimal to double and back.

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DECIMAL_DIG was deemed more useful than FP_CONV_DIG, which previous versions of this document defined as the number of decimal digits for which the implementation guaranteed correctly rounded conversion.

For IEEE Implementations

Conversion from the widest supported IEEE standard format to decimal with DECIMAL_DIG digits and back is the identity function. See §4.2.1.2 and 4.2.2.1 20 regarding conversion requirements.

Examples

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If the minimum-width IEEE 754 extended format (64 bits of precision) is supported, DECIMAL_DIG must be at least 21. If IEEE 754 double (53 bits of precision) is the widest IEEE format supported, then DECIMAL_DIG must be at least 17. By contrast, LDBL_DIG and DBL_DIG are 19 and 15, respectively, for these formats.

4.3.1 Overloaded functions 30

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The specification of the header <fp. h> uses the notion of overloaded functions. The function designators are overloaded with multiple prototypes which become declared when <fp.h> is included. They are used much like ordinary functions, but they behave more like typical built-in arithmetic operators: their semantic type is affected by their arguments; their result is at least as wide as the minimum evaluation format; and, with widest-need expression evaluation, the evaluation format propagates from the call to its arguments.

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For each overloaded function defined in this section, the implementation provides a set of functions—one for the minimum evaluation format and one for each wider floating format. Their prototypes are identical except for their floating-point return type and one or more overloading parameters whose type is identical to the return type. Prototypes have the form

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floating-type function-designator (argument-list) ;

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Subsequent sections give a form in this style for each overloaded function. The form determines the required prototypes.

Example

The square root function has the prototype form

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floating-type sqrt(floating-type x);

So, if the minimum evaluation format were float then the implementation would have

```
float sqrt(float);
double sqrt(double);
long double sqrt(long double);
```

Example

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10 The remous function has the form

```
floating-type remquo(floating-type x, floating-type y, int *quo);
```

So, if the minimum evaluation format were double then the implementation would have

```
double remquo(double, double, int *);
long double remquo(long double, long double, int *);
```

- A function call that is compatible with one of the prototypes for an overloaded function is compatible with all of them. For such a function call, occurring after inclusion of <fp.h> in the translation unit, the implementation determines the evaluation format for the call and chooses the matching prototype. First, any integer arguments for the overloading parameters are converted to double. Then the evaluation format for the call is determined to be the widest of
 - 1. the arguments for the overloading parameters,
 - 2. the minimum evaluation format,

and in the case of widest-need (§3.2.3.1)

- 3. any evaluation format propagated down to the call.
- With widest-need expression evaluation, the evaluation format for the call, which matches the type of the invoked function, is propagated through the call to the arguments corresponding to the overloading parameters.
- Taking the address of an overloaded function or passing it as an argument to a function results in undefined behavior.

Overloaded functions cooperate with expression evaluation methods much as arithmetic operators do. For example, with

the type of sqrt and evaluation format of + actually used are:

50	min-eval-format	widest-need	sort()	f + f
	float	no	float	float
	double	no	double	double
	long double	either	long double	long double
55	float	yes	double	double
	double	yes	double	double

Modeled after C++, the rudimentary overloading required by this specification can reasonably be expected to be compatible with future overloading extensions to C. General purpose overloading for C is beyond the scope of this document.

This specification does not prescribe any particular implementation mechanism. It could be implemented simply with built-in macros. A function such as

floating-type sqrt(floating-type);

10 could be implemented with

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```
#undef sqrt
#define sqrt(x) __BUILTIN_OVERLOAD_sqrt(x)
```

Note that implementations whose minimum evaluation format is long double require no overloading mechanism since only one prototype, the long double one, is needed for each function.

This specification borrows heavily from [14] and [15]. [15] is functionally similar, but is presented in the style of Fortran generic intrinsic functions. Like this specification, [14] is consistent with C++ overloading. Adding a suitable subset of C++ overloading to C, as prescribed by [14], would support the overloading required here, and as well provide a useful user-extensible overloading mechanism. (With the current C++ overloading rules, additional prototypes would be required to handle integer arguments. [14] suggests how C++ overloading might be extended to accommodate widest-need.)

The C* language, an extended C, includes a function overloading scheme that supports its parallel types. The C* definition in [21] differs from this specification and current C++ in that its overloading resolution depends on the order of parameters.

The great majority of existing C programs are expected to run correctly straightaway when <fp.h> is included instead of <math.h>. Overloaded functions differ from corresponding Standard C library functions essentially only in the semantic types of return values.

Use of Standard C's reserved f and 1 suffixed identifiers could be supported with macros such as

```
#define sinf(x) sin((float)(x))
```

40 (Taking the address of such a function or passing it as an argument would be disallowed.)

The ability to overload on integer as well as floating types would have been useful for some functions, for example copysign. Overloading with different numbers of arguments would have allowed reusing names, for example remainder for remquo. However, these facilities would have complicated the specification somewhat and their natural consistent use, such as for a floating abs or a two argument atan, would have introduced further inconsistencies with Standard C for insufficient benefit.

This specification in no way limits the implementation's options for efficiency, including inlining library functions (ISO §7.1.6; ANSI §4.1.6).

4.3.2 Trigonometric functions (ISO §7.5.2; ANSI §4.5.2)

The header <fp.h> declares overloaded versions of all the Standard C trigonometric functions.

```
4.3.2.1 The acos function (ISO §7.5.2.1; ANSI §4.5.2.1)
      Synopsis
5
          #include <fp.h>
          floating-type acos(floating-type x);
     4.3.2.2 The asin function (ISO §7.5.2.2; ANSI §4.5.2.2)
10
      Synopsis
          #include <fp.h>
          floating-type asin(floating-type x);
     4.3.2.3 The atan function (ISO §7.5.2.3; ANSI §4.5.2.3)
15
      Synopsis
          #include <fp.h>
20
          floating-type atan(floating-type x);
     4.3.2.4 The atan2 function (ISO §7.5.2.4; ANSI §4.5.2.4)
      Synopsis
25
          #include <fp.h>
          floating-type atan2(floating-type y, floating-type x);
     4.3.2.5 The cos function (ISO §7.5.2.5; ANSI §4.5.2.5)
30
      Synopsis
          #include <fp.h>
          floating-type cos(floating-type x);
35
           The sin function (ISO §7.5.2.6; ANSI §4.5.2.6)
      Synopsis
40
          #include <fp.h>
           floating-type sin(floating-type x);
     4.3.2.7 The tan function (ISO §7.5.2.7; ANSI §4.5.2.7)
45
      Synopsis
           #include <fp.h>
           floating-type tan(floating-type x);
50
    4.3.3
            Hyperbolic functions (ISO §7.5.3; ANSI §4.5.3)
       The header <fp.h> declares overloaded versions of the Standard C hyperbolic
```

functions and their arc counterparts.

4.3.3.1 The acosh function IRMA (LEAN) DRIVE DRIVE BOOK BOTT LEAN

Synopsis

#include <fp.h>
floating-type acosh(floating-type x);

Description

The acosh function computes the (nonnegative) are hyperbolic cosine of x.

Returns

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The acosh function returns the arc hyperbolic cosine.

4.3.3.2 The asinh function

Synopsis

#include <fp.h>
floating-type asinh(floating-type x);

Description

The asinh function computes the arc hyperbolic sine of x.

Returns

The asinh function returns the arc hyperbolic sine.

4.3.3.3 The atanh function

Synopsis

#include <fp.h>
floating-type atanh(floating-type x);

Description

The atanh function computes the arc hyperbolic tangent of x.

Returns

The atanh function returns the arc hyperbolic tangent.

4.3.3.4 The cosh function (ISO §7.5.3.1; ANSI §4.5.3.1)

Synopsis

#include <fp.h>
floating-type cosh(floating-type x);

4.3.3.5 The sinh function (ISO §7.5.3.2; ANSI §4.5.3.2)

Synopsis

#include <fp.h>
floating-type sinh(floating-type x);

4.3.3.6 The tanh function (ISO §7.5.3.3; ANSI §4.5.3.3)

10 Synopsis

#include <fp.h>
floating-type tanh(floating-type x);

15 4.3.4 Exponential and logarithmic functions (ISO §7.5.4; ANSI §4.5.4

The header <fp.h> declares overloaded versions of the Standard C exponential and logarithmic functions—except for modf which is declared but not overloaded—and several related functions.

4.3.4.1 The exp function (ISO §7.5.4.1; ANSI §4.5.4.1)

25 Synopsis

#include <fp.h>
floating-type exp(floating-type x);

30 **4.3.4.2** The exp2 function

Synopsis

#include <fp.h>
35 floating-type exp2(floating-type x);

Description

The exp2 function computes the base-2 exponential of x: 2x.

Returns

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The exp2 function returns the base-2 exponential.

45 **4.3.4.3** The expm1 function

Synopsis

#include <fp.h>
floating-type expml(floating-type x);

Description

The expm1 function computes the base-e exponential of the argument, minus 1: $e^{x} - 1$. For small magnitude x, expm1(x) is expected to be more accurate than exp(x) - 1.

Returns

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The expm1 function returns ex - 1.

4.3.4.4 The frexp function (ISO §7.5.4.2; ANSI §4.5.4.2)

Synopsis

#include <fp.h>
floating-type frexp(floating-type value, int *exp);

4.3.4.5 The Idexp function (ISO §7.5.4.3; ANSI §4.5.4.3)

20 Synopsis

#include <fp.h>
floating-type ldexp(floating-type x, int exp);

25 4.3.4.6 The log function (ISO §7.5.4.4; ANSI §4.5.4.4)

Synopsis

#include <fp.h>
floating-type log(floating-type x);

4.3.4.7 The log10 function (ISO §7.5.4.5; ANSI §4.5.4.5)

Synopsis

#include <fp.h>
floating-type log10(floating-type x);

4.3.4.8 The log1p function

Synopsis

#include <fp.h>
floating-type log1p(floating-type x);

Description

The log1p function computes the base-e logarithm of 1 plus the argument. For small magnitude x, log1p(x) is expected to be more accurate than log(1 + x).

Returns

The log1p function returns the base-e logarithm of 1 plus the argument.

4.3.4.9 The log2 function

Synopsis

#include <fp.h>
floating-type log2(floating-type x);

Description

The log2 function computes the base-2 logarithm of x.

Returns

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The log2 function returns the base-2 logarithm.

4.3.4.10 The logb function

Synopsis

#include <fp.h>
floating-type logb(floating-type x);

Description

- The logb function extracts the exponent of x, as a signed integral value in the format of x. If x is subnormal it is treated as though it were normalized; thus for positive finite x,
 - 1 S x * FLT_RADIX-logb(x) < FLT_RADIX
- The treatment of subnormal x follows the recommendation in IEEE standard 854, which differs from IEEE standard 754 on this point. Even 754 implementations should follow this definition rather than the one recommended (not required) by 754.
- Particularly on machines whose radix is not 2, logb can be expected to obtain the exponent more accurately and quickly than frexp.

Returns

The logb function returns the signed exponent of its argument.

4.3.4.11 The modf functions (ISO §7.5.4.7; ANSI §4.5.4.6)

Synopsis

- #include <fp.h>
 double modf(double value, double *iptr);
 float modff(float value, float *iptr);
 long double modfl(long double value, long double *iptr);
- 50 4.3.4.12 The scalb function

Synopsis

#include <fp.h>
55 floating-type scalb(floating-type x, long int n);

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Description

The scalb function computes $x * FLT_RADIX^n$ efficiently, not normally by computing FLT_RADIX^n explicitly.

Returns

The scalb function returns $x * FLT_RADIX^n$.

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On machines whose radix is not 2, scalb, compared with ldexp, can be expected to have better accuracy, speed, and overflow and underflow behavior.

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The second parameter has type long int, unlike the corresponding int parameter for ldexp, because the factor required to scale from the smallest positive floating-point value to the largest finite one, on many implementations, is too large to represent in the minimum-width int format allowed by Standard C.

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4.3.5 Power and absolute value functions (ISO §7.5.5, 7.5.6; ANSI §4.5.5, 4.5.6)

The header <fp.h> declares overloaded versions of the Standard C power and absolute value functions and a hypotenuse function.

25 4.3.5.1 The fabs function (ISO §7.5.6.2; ANSI §4.5.6.2)

Synopsis

#include <fp.h>

floating-type fabs(floating-type x);

4.3.5.2 The hypot function

Synopsis

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```
#include <fp.h>
floating-type hypot(floating-type x, floating-type y);
```

Description

The hypot function computes the square root of the sum of the squares of x and y, without undue overflow or underflow.

Returns

The hypot function returns the square root of the sum of the squares of x and y.

4.3.5.3 The pow function (ISO §7.5.5.1; ANSI §4.5.5.1)

50 Synopsis

```
#include <fp.h>
floating-type pow(floating-type x, floating-type y);
```

4.3.5.4 The sqrt function (ISO §7.5.5.2; ANSI §4.5.5.2) Synopsis 5 #include <fp.h> floating-type sqrt(floating-type x); 4.3.6 Error and gamma functions 10 See [23] regarding implementation. 4.3.6.1 The erf function 15 Synopsis #include <fp.h> floating-type erf(floating-type x); 20 Description The erf function computes the error function of x. Returns 25 The erf function returns the error function of x. 4.3.6.2 The erfc function 30 Synopsis #include <fp.h> floating-type erfc(floating-type x); 35 Description The erfc function computes the complementary error function of x. Returns The erfc function returns the complementary error function of x. 4.3.6.3 The gamma function Synopsis

50 Description

#include <fp.h>

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The gamma function computes the gamma function of x: $\Gamma(x)$.

floating-type gamma(floating-type x);

Returns

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The gamma function returns $\Gamma(x)$.

In UNIX System V [10], both the gamma and lgamma functions compute $log_e(|\Gamma(x)|)$.

4.3.6.4 The Igamma function

Synopsis

#include <fp.h>
floating-type lgamma(floating-type x);

Description

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The 1gamma function computes the logarithm of the absolute value of gamma of x: $log_e(|\Gamma(x)|)$.

In UNIX System V [10], a call to 1gamma sets an external variable signgam to the sign of gamma (x), which is -1 if

x < 0 && remainder(floor(x), 2) != 0

Note that this specification does not remove the external identifier signgam from the user's name space. An implementation that supports, as an extension, lgamma's setting of signgam must still protect the external identifier signgam if defined by the user.

Returns

The 1gamma function returns $\log_e(|\Gamma(x)|)$.

4.3.7 Nearest integer functions (ISO §7.5.6; ANSI §4.5.6)

The header <fp.h> declares overloaded versions of the Standard C nearest integer functions, nearest integer functions specified by the IEEE standards, and functions similar to common Fortran nearest integer functions.

4.3.7.1 The ceil function (ISO §7.5.6.1; ANSI §4.5.6.1)

Synopsis

#include <fp.h>
floating-type ceil(floating-type x);

4.3.7.2 The floor function (ISO §7.5.5.1; ANSI §4.5.5.1)

Synopsis

#include <fp.h>
floating-type floor(floating-type x);

4.3.7.3 The nearbyint function

Synopsis

#include <fp.h>
floating-type nearbyint(floating-type x);

Description

The nearbyint function differs from the rint function (§4.3.7.4) only in that the nearbyint function does not raise the inexact exception. (See §F.6.3-4.)

For implementations that do not support the inexact exception, nearbyint and rint are equivalent.

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Returns

The nearbyint function returns the rounded integral value.

20 **4.3.7.4** The rint function

Synopsis

#include <fp.h>
25 floating-type rint(floating-type x);

Description

The rint function rounds its argument to an integral value in floating-point format, using the current rounding direction.

Returns

The rint function returns the rounded integral value.

35

4.3.7.5 The rinttol function

Synopsis

#include <fp.h>
long int rinttol(long double x);

Description

The rinttol function rounds its argument to the nearest long int, rounding according to the current rounding direction. If the rounded value is outside the range of long int, the numeric result is unspecified.

Returns

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The rinttol function returns the rounded long int value, using the current rounding direction.

4.3.7.6 The round function

Synopsis

5 #incl

#include <fp.h>
floating-type round(floating-type x);

Description

The round function rounds its argument to the nearest integral value in floating-point format, using add half to the magnitude and chop rounding a la the Fortran anint function, regardless of the current rounding direction.

Returns

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The round function returns the rounded integral value.

4.3.7.7 The roundtol function when believes and account and adversarial and account account and account and account and account and account and account account and account and account account account and account account and account account account and account account account account and account accoun

20 Synopsis

```
#include <fp.h>
long int roundtol(long double x);
```

25 Description

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The roundtol function returns the rounded long int value, using add half to the magnitude and chop rounding a la the Fortran nint function and the Pascal round function, regardless of the current rounding direction. If the rounded value is outside the range of long int, the numeric result is unspecified.

Returns

The roundtol function returns the rounded long int value.

4.3.7.8 The trunc function

Synopsis

#include <fp.h>
floating-type trunc(floating-type x);

Description

The trunc function rounds its argument to the integral value, in floating format, nearest to but no larger in magnitude than the argument.

Returns

The trunc function returns the truncated integral value.

4.3.8 Remainder functions (ISO §7.5.6; ANSI §4.5.6)

The header <fp.h> declares an overloaded Standard C fmod function and two versions of the IEEE floating-point standards' remainder function.

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4.3.8.1 The fmod function (ISO §7.5.6.4; ANSI §4.5.6.4)

Synopsis

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```
#include <fp.h>
floating-type fmod(floating-type x, floating-type y);
```

4.3.8.2 The remainder function

15 Synopsis

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Description

The remainder function computes the remainder x REM y required by the IEEE floating-point standards.

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"When $y \neq 0$, the remainder r = x REM y is defined regardless of the rounding mode by the mathematical relation $r = x \cdot y * n$, where n is the integer nearest the exact value of x/y; whenever $|n \cdot x/y| = 1/2$, then n is even. Thus, the remainder is always exact. If r = 0, its sign shall be that of x." [3] §5.1.

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(This definition can be implemented for non-IEEE as well as IEEE machines.)

Returns

The remainder function returns x REM y.

4.3.8.3 The remquo function

Synopsis

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45 Description

The remaple function computes the same remainder as the remainder function. In the object pointed to by quo it stores a value whose sign is the sign of x/y and whose magnitude is congruent mod 2^n to the magnitude of the integral quotient of x/y, where n is an implementation-defined integer at least 3.

Returns

The remquo function returns x REM y.

The remquo function is intended for implementing argument reductions, which can exploit a few low-order bits of the quotient. Note that x may be so large in magnitude relative to y that an exact representation of the quotient is not practical.

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4.3.9 Manipulation functions

The copysign function

These extension functions manipulate representations of floating-point numbers.

10 **4.3.9.1**

Synopsis

```
#include <fp.h>
floating-type copysign(floating-type x, floating-type y);
```

Description

The copys
20 produces a

The copysign function produces a value with the magnitude of x and the sign of y. It produces a NaN (with the sign of y) if x is a NaN. On implementations that represent a signed zero but do not treat negative zero consistently in arithmetic operations, the copysign function regards the sign of zero as positive.

The requirement that copysign regard a negative sign of zero as positive if the arithmetic treats negative zero like positive zero is justified in order to preserve more identities. For example, to preserve the identity, the square root of the product is the product of the square roots, the algorithm in [22] for the complex square root depends on consistency of copysign with the rest of the arithmetic: if -0 behaves like +0 then the square root of the product would yield

 $\sqrt{3*(-1-0i)} = \sqrt{-3+0i} \rightarrow 0 + \sqrt{3}i$

but if copysign were to treat the sign of -0 as negative then the product of the square roots would yield

 $\sqrt{3} * \sqrt{-1 - 0i} \rightarrow \sqrt{3} * (0 - i) = 0 - \sqrt{3}i$

Returns

The copysign function returns a value with the magnitude of x and the sign of y.

4.3.9.2 The nan functions

Synopsis

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```
#include <fp.h>
double nan(const char *tagp);
float nanf(const char *tagp);
long double nanl(const char *tagp);
```

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Description

If the implementation supports quiet NaNs in the type of the function, then the call nan("n-char-sequence") is equivalent to strtod("NAN(n-char-sequence)",

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(char**) NULL); the call nan("") is equivalent to strtod("NAN()", (char**) NULL). Similarly nanf and nanl are defined in terms of strtof and strtold. If tagp does not point to an n-char-sequence string then the result NaN's content is unspecified. A call to a nan function of a type for which the implementation does not support quiet NaNs is unspecified.

Returns

The nan functions return a quiet NaN, if available, with content indicated through tagp.

4.3.9.3 The nextafter functions

Synopsis

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#include <fp.h>
floating-type nextafter(floating-type x, long double y);
float nextafterf(float x, float y);
double nextafterd(double x, double y);
long double nextafterl(long double x, long double y);

Description

The nextafter functions determine the next representable value, in the type of the function, after x in the direction of y. The nextafter functions return y if x == y.

Returns

The nextafter functions return the next representable value after x in the direction of y.

It's sometimes desirable to find the next representation after a value in the direction of a previously computed value—maybe smaller, maybe larger. The nextafter functions have a second floating argument so that the program will not have to include floating-point tests for determining the direction in such situations. And, on some machines these tests may fail due to overflow, underflow, or roundoff.

The overloaded nextafter function depends substantially on the expression evaluation method—which is appropriate for certain uses but not for others. The explicitly typed functions can be employed to obtain next values in a particular format. For example,

```
nextafterf(x, y)
```

will return the next float value after (float) x in the direction of (float) y regardless of the evaluation method.

The second parameter of the overloaded nextafter function has type long double primarily to keep the overloading scheme simple. Promotion of the second argument to long double is harmless but unnecessary.

For the case x == y, the IEEE floating-point standards recommend that x be returned. This specification differs in order that nextafter(-0.0, +0.0) return +0.0 and nextafter(+0.0, -0.0) return -0.0.

4.3.10 Maximum, minimum, and positive difference functions

These extension functions correspond to standard Fortran functions, dim, max, and min [16].

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Their names have f prefixes to allow for integer versions—following the example of fabs and abs.

4.3.10.1 The fdim function

Synopsis

```
#include <fp.h>
floating-type fdim(floating-type x, floating-type y);
```

Description

The fdim function determines the positive difference between its arguments:

Returns

The fdim function returns the positive difference between x and y.

4.3.10.2 The fmax function

Synopsis

#include <fp.h>
floating-type fmax(floating-type x, floating-type y);

Description

The fmax function determines the maximum numeric value of its arguments.

NaN arguments should be treated as missing data. If one argument is a NaN and the other numeric, then fmax should chose the numeric value. (See §F.9.2.)

Returns

The fmax function returns the maximum numeric value of its arguments.

45 4.3.10.3 The fmin function

Synopsis

#include <fp.h>
floating-type fmin(floating-type x, floating-type y);

Description

The fmin function determines the minimum numeric value of its arguments.

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NaN arguments should be treated as missing data. If one argument is a NaN and the other numeric, then fmin should chose the numeric value. (See §F.9.3.)

5 Returns

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The fmin function returns the minimum numeric value of its arguments.

4.4 Floating-Point Environment <fenv.h>

The header <fenv.h> declares two types and several macros and functions to provide access to the floating-point environment.

Names of macros and functions in this section consistently include an FE_ or fe prefix and employ certain abbreviations. The prefix calls attention to environmental access functions, which require an enabling fenv_access pragma (see §2). The abbreviations env and except are used in Standard C and UNIX System V, respectively.

The interface described here is not intended to support trap handlers, which are outside the scope of this document.

The typedef

fenv_t

is a type for representing the entire floating-point environment.

The typedef

30 fexcept_t

is a type for representing the floating-point exception flags collectively, including any status the implementation associates with the flags.

See rationale in §4.4.1.

Each macro

FE_INEXACT
FE_DIVBYZERO
FE_UNDERFLOW
FE_OVERFLOW
FE_INVALID

is defined if and only if the implementation supports the exception by means of the functions in §4.4.1. The defined macros expand to int constant expressions whose values are distinct powers of 2, all suitable for use in #if preprocessing directives.

The macro

FE_ALL_EXCEPT

is simply the bitwise OR of all exception macros defined by the implementation.

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Each macro

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FE_TONEAREST FE_UPWARD FE_DOWNWARD FE_TOWARDZERO

is defined if and only if the implementation supports getting and setting the represented rounding direction by means of the fegetround and fesetround functions. The defined macros expand to int constant expressions whose values are distinct nonnegative values, all suitable for use in #if preprocessing directives.

The rounding direction macros might expand to constants corresponding to the values of FLT_ROUNDS, the Standard C inquiry for the rounding direction of addition, but need not.

The macro

FE_DFL_ENV

represents the default floating-point environment—the one installed at program startup—and has type pointer to fenv_t. It can be used as an argument to <fenv.h> functions that manage the floating-point environment.

Unsupported macros are not defined in order to assure that their use results in a translation error. A program might explicitly define such macros, to allow translation of code (perhaps never executed) containing the macros. An unsupported exception macro should be defined to be 0, for example

#ifndef FE_INEXACT
#define FE_INEXACT 0
#endif

so that a bitwise OR of macros has a reasonable effect.

35 **4.4.1** Exceptions

The following functions provide access to the exception flags. The int input argument for the functions represents a subset of floating-point exceptions, and can be constructed by bitwise ORs of the exception macros, for example FE_OVERFLOW | FE_INEXACT. For other argument values the behavior of these functions is undefined.

The IEEE standards require that exception flags represent, at least, whether the flag is set or clear; the functions fetestexcept, feraiseexcept, and feclearexcept support this basic abstraction. However, an implementation may endow exception flags with more information—for example, the address of the code which raised the exception; the functions fegetexcept and fesetexcept deal with the full content of flags.

In previous drafts of this specification, several of the exception functions returned an int indicating whether the excepts argument represented supported exceptions. This facility was deemed unnecessary because excepts & ~FE_ALL_EXCEPT can be used to test invalidity of the excepts argument.

4.4.1.1 The feclear except function

Synopsis

#include <fenv.h>
void feclearexcept(int excepts);

Description

The feclear except function clears the supported exceptions represented by its argument. The argument excepts represents exceptions as a bitwise OR of exception macros.

4.4.1.2 The fegetexcept function

Synopsis

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#include <fenv.h>
void fegetexcept(fexcept_t *flagp, int excepts);

Description

The fegetexcept function stores an implementation-defined representation of the exception flags indicated by the argument excepts through the pointer argument flagp.

4.4.1.3 The feraiseexcept function

Synopsis

#include <fenv.h>
void feraiseexcept(int excepts);

Description

The feraiseexcept function raises the supported exceptions represented by its argument. The argument excepts represents exceptions as a bitwise OR of exception macros. The order in which these exceptions are raised is unspecified.

It is intended that enabled traps for exceptions raised by the feraiseexcept function are taken.

For IEEE Implementations

- If the argument excepts represents coincident exceptions that are valid for atomic operations—namely overflow and inexact, or underflow and inexact—then overflow or underflow is raised before inexact.
- The function is not restricted to accept only valid coincident expressions for atomic operations, so that the function can be used to raise exceptions accrued over several operations.

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4.4.1.4 The fesetexcept function

Synopsis

#include <fenv.h>
void fesetexcept(const fexcept_t *flagp, int excepts);

Description

The fesetexcept function sets the complete status for those exception flags indicated by the argument excepts, according to the representation in the object pointed to by flagp. The value of *flagp must have been set by a previous call to fegetexcept; if not, the effect on the indicated exception flags is undefined. This function does not raise exceptions, but only sets the state of the flags.

4.4.1.5 The fetestexcept function

Synopsis

#include <fenv.h>
int fetestexcept(int excepts);

Description

The fetestexcept function determines which of a specified subset of the exception flags are currently set. The excepts argument specifies—as a bitwise OR of the exception macros—the exception flags to be queried.

Returns

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The fetestexcept function returns the bitwise OR of the exception macros corresponding to the currently set exceptions included in excepts.

Example

Call f if invalid is set, g if overflow is set:

```
#pragma fenv_access on
int set_excepts;
set_excepts = fetestexcept(FE_INVALID | FE_OVERFLOW);
if (set_excepts & FE_INVALID) f();
if (set_excepts & FE_OVERFLOW) g();
```

This mechanism allows testing several exceptions with just one function call. The argument is a *mask* because querying all flags may be more expensive on some architectures.

4.4.2 Rounding

The fegetround and fesetround functions provide control of rounding direction modes.

The IEEE floating-point standards prescribe rounding precision modes (in addition to the rounding direction modes covered by the functions in this section) as a means for systems

whose results are always double or extended to mimic systems that deliver results to narrower formats. An implementation of C can meet this goal in any of the following ways:

- By supporting the float minimum evaluation format (see §3.2.3).
 - 2. By providing pragmas or compile options to shorten results by rounding to IEEE single or double precision.
- 3. By providing functions to set and get, dynamically, rounding precision modes which shorten results by rounding to IEEE single or double precision. Recommended are functions fesetprec and fegetprec and macros FE_FLTPREC, FE_DBLPREC, and FE_LDBLPREC, analogous to the functions and macros for the rounding direction modes.
- This specification does not include a portable interface for precision control because the IEEE floating-point standards are ambivalent on whether they intend for precision control to be dynamic (like the rounding direction modes) or static. Indeed, some floating-point architectures provide control modes, suitable for a dynamic mechanism, and others rely on instructions to deliver single- and double-format results, suitable only for a static mechanism.

4.4.2.1 The fegetround function

Synopsis

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#include <fenv.h>
int fegetround(void);

Description

The fegetround function gets the current rounding direction.

Returns

The fegetround function returns the value of the rounding direction macro representing the current rounding direction.

4.4.2.2 The fesetround function

40 Synopsis

#include <fenv.h>
int fesetround(int round);

45 Description

The fesetround function establishes the rounding direction represented by its argument round. If the argument does not match a rounding direction macro, the rounding direction is not changed.

Returns

The fesetround function returns a nonzero value if and only if the argument matches a rounding direction macro (that is, if and only if the requested rounding direction can be established).

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Example

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Save, set, and restore the rounding direction. Report an error and abort if setting the rounding direction fails.

#pragma fenv_access on
int save_round;
save_round = fegetround();
int setround_ok = fesetround(FE_UPWARD);
assert(setround_ok);
. . .
fesetround(save_round);

4.4.3 Environment

The functions in this

The functions in this section manage the floating-point environment—exception flags, dynamic rounding modes, and any dynamic modes for handling floating-point exceptions—as one entity.

20 4.4.3.1 The fegetenv function

Synopsis

#include <fenv.h>
25 void fegetenv(fenv_t *envp);

Description

The fegetenv function stores the current floating-point environment in the object pointed to by envp.

4.4.3.2 The feholdexcept function

Synopsis

#include <fenv.h>
int feholdexcept(fenv_t *envp);

Description

The feholdexcept function saves the current environment in the object pointed to by envp, clears the exception flags, and installs the non-stop mode, if available, for all exceptions. For implementations whose floating-point environment contains modes for exception handling, including a non-stop (continue on exceptions) mode, the feholdexcept function can be used in conjunction with the feupdateenv function to write routines that hide spurious exceptions from their callers.

Returns

The feholdexcept function returns nonzero if and only if non-stop exception handling was successfully installed.

feholdexcept should be effective on typical IEEE implementations which have the default non-stop mode and at least one other mode for trap handling or aborting. If the

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implementation provides only the non-stop mode then installing the non-stop mode is trivial.

More appropriate for the user model prescribed in §2, feholdexcept supersedes feprocentry which is equivalent to

```
fegetenv(envp);
fesetenv(FE_DFL_ENV);
```

10 4.4.3.3 The fesetenv function

Synopsis

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#include <fenv.h>
15 void fesetenv(const fenv_t *envp);

Description

The fesetenv function establishes the floating-point environment represented by the object pointed to by envp. The argument envp must point to an object set by a call to fegetenv, or equal the macro FE_DFL_ENV or an implementation-defined value of type pointer to fenv_t. Note that fesetenv merely installs the state of the exception flags represented through its argument, and does not raise these exceptions.

25 4.4.3.4 The feupdateenv function

Synopsis

#include <fenv.h>
void feupdateenv(const fenv_t *envp);

Description

The feupdateenv function saves the current exceptions in its automatic storage, installs the environment represented through envp, and then raises (actually re-raises) the saved exceptions. For implementations whose floating-point environment contains modes for exception handling, including a non-stop (continue on exceptions) mode, the feupdateenv function can be used in conjunction with the feholdexcept function to write routines that hide spurious exceptions from their callers.

feupdateenv was called feprocexit in earlier drafts of this specification.

Example

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45 Hide spurious underflow exceptions:

APPENDIXES

Language Syntax Extensions (ISO §B; ANSI §A)

5 This appendix summarizes language syntax extensions to Standard C.

Constants (ISO §B.1.4; ANSI §A.1.4)

floating-constant:

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hexadecimal-floating-constant

hexadecimal-floating-constant:

0x hexadecimal-fractional-constant binary-exponent-part floating-suffixont

ox hexadecimal-fractional-constant binary-exponent-part floating-suffixont

0x hexadecimal-digit-sequence binary-exponent-part floating-suffixont

ox hexadecimal-digit-sequence binary-exponent-part floating-suffixont

hexadecimal-fractional-constant:

hexadecimal-digit-sequence hexadecimal-digit-sequence

hexadecimal-digit-sequence.

hexadecimal-digit-sequence:

hexadecimal-digit

hexadecimal-digit-sequence hexadecimal-digit

binary-exponent-part:

p signopt digit-sequence

signopt digit-sequence

Operators (ISO §B.1.6; ANSI §A.1.6)

operator: one of

!<>= <>= !<= !< !>= !> !<>

Preprocessor Numbers (ISO §B.1.9; ANSI §A.1.9)

pp-number:

pp-number

pp-number sign

A.4 Relational Expressions (ISO §B.2.1; ANSI §A.2.1)

relational expression:

```
shift-expression
             relational-expression
                                      !<>=
5
                                             shift-expression
             relational-expression
                                      <>
                                             shift-expression
             relational-expression
                                      <>=
                                             shift-expression
              relational-expression
                                      !<=
              relational-expression
                                             shift-expression
                                      !<
                                             shift-expression
              relational-expression
10
                                      !>=
                                             shift-expression
              relational-expression
                                      !>
                                             shift-expression
              relational-expression
                                      !<>
```

A.5 Pragmas

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#pragma fenv_access on-off-switch

on-off-switch: one of:
on off default

#pragma fp_contract on-off-switch

#pragma fp_wide_function_returns on-off-switch
#pragma fp_wide_function_parameters on-off-switch
#pragma fp_wide_variables on-off-switch

B. Optimization

Many common optimizations for integer arithmetic are not generally valid (nor as useful) for floating-point. This appendix is an implementation note explaining some of the constraints.

B.1 Expression evaluation

35 For IEEE Implementations

Floating-point arithmetic operations and external function calls may entail side effects which optimization must honor, at least within the scope of an enabling fenv_access pragma (§2). The flags and modes in the floating-point environment may be regarded as global variables; floating-point operations (+, *, etc.) implicitly read the modes and write the flags.

Concern about side effects may inhibit code motion, removal of useless code, and certain transformations. For example, in

```
#pragma fenv_access on
double x;
...
for (i = 0; i < n; i++) x + 1;</pre>
```

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x + 1 might overflow, so cannot be removed. And since the loop body might not execute (maybe $0 \ge n$), x + 1 cannot be moved out of the loop. Of course these optimizations are valid if the implementation can rule out the nettlesome cases.

Within a basic block exceptions need not be precise. Thus the preceding loop could be treated as

if (0 < n) x + 1;

10 B.2 Expression transformations

The following transformations are not generally valid.

Removal of parentheses. This is invalid for any floating-point arithmetic. In particular, the implementation cannot apply the associative laws for + and *.

Factoring. Application of the distributive law is invalid for any floating-point arithmetic. For example, the implementation cannot replace x + x * y by x * (1.0 + y).

- $x x \rightarrow 0$. The expressions x x and 0 are not equivalent if x is a NaN or infinite. (Of course, the two expression are not equivalent if x has side-effects.)
- $x-y \leftrightarrow -(y-x)$. For IEEE machines, in the default rounding direction, 1-1 is +0 but -(1-1) is -0. The expressions x-y and -(y-x) are not equivalent on the CDC CYBER 205, because of abuse of 1's complement arithmetic. On the other hand, the expressions x-y, x+(-y), and (-y)+x are equivalent on IEEE machines, among others.
- $x/5.0 \leftrightarrow x * 0.2$. Such transformations involving constants generally do not yield numerically equivalent expressions. If the constants are exact then such transformations can be made on IEEE machines and others that round perfectly.
 - $0 * x \rightarrow 0$. The expressions 0 * x and 0 are not equivalent if x is a NaN or infinite.
 - $l * x, x/l \rightarrow x$. Neither 1 * x and x nor x / 1 and x are equivalent if x has almost overflowed on a CRAY-1 or CRAY-2 or if x has almost underflowed on a CDC CYBER 170.
- $x + 0 \rightarrow x$. For IEEE machines, if x is -0 then, in the default rounding direction, x + (+0) yields +0, not x; the implementation cannot replace x + 0 by x unless it can determine that x cannot be -0.
- $x 0 \rightarrow x$. For IEEE machines, (+0) (+0) yields -0 when rounding is downward (toward $-\infty$), but +0 otherwise, and (-0) (+0) always yields -0; so, if the state of fenv_access were off, promising default rounding, then the implementation could replace x 0 by x, even if x might be zero.
- $-x \leftrightarrow 0 x$. For IEEE machines, -(+0) yields -0, but 0 (+0) yields +0 (unless rounding is downward); the expressions are numerically equivalent for all other cases.

20

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The IEEE floating-point standards prescribe a signed zero to preserve mathematical identities across certain discontinuities. Examples include

```
1 / (1 / (±INFINITY)) is ±INFINITY complex_conjugate(sqrt(z)) is sqrt(complex_conjugate(z))
```

B.3 Relational operators

- $x != x \rightarrow false$. In IEEE implementations, the statement x != x is true if x is a NaN. In non-IEEE implementations with NaNs (reserved operands, indefinites) x != x may trap.
- $x == x \rightarrow true$. In IEEE implementations, the statement x == x is false if x is a NaN. In non-IEEE implementations with NaNs (reserved operands, indefinites) x == x may trap.
 - $x ! op y \leftrightarrow !(x op y)$. Though equal these expressions are not equivalent on IEEE implementations if op includes < or >, x or y might be a NaN, and the state of fenv_access is on.
- $x \circ p y \to !(x ! \circ p y)$. This transformation, which would be desirable if extra code were required to cause the invalid exception for unordered cases, could be performed provided the state of fenv_access is off.
- The sense of relational operators must be maintained. For IEEE implementations, this includes handling unordered cases as expressed by the source code. (Handling relationals correctly might not require generating worse code.)

Example

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is not equivalent to

nor to

- nor, unless the state of fenv_access is off, to

but is equivalent to

if (!(a < b)) g(); else f();</pre>

B.4 Constant arithmetic

Under the effect of an enabling fenv_access pragma, the implementation must honor exceptions raised because of execution-time constant arithmetic. See §3.4, 3.5. Even under the effect of an enabling fenv_access pragma, an operation on constants that raises no exception can be folded during translation; implementations that support dynamic rounding precision modes (§4.4.2) should assure further that the result of the operation raises no exception when converted to the semantic type of the operation.

10 B.5 Wide representation

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Implementations employing wide registers must take care to honor appropriate semantics. Values must be independent of whether they are represented in a register or in memory. For example, an implicit spilling of a register must not alter the value. Also, an explicit store and load must round to the precision of the storage type. In particular, casts and assignments must perform their specified conversion (ISO §6.2.1.5; ANSI §3.2.1.5): for

```
double d1, d2;
20 float f;
d1 = f = expression;
d2 = (float)expression;
```

the values assigned to d1 and d2 must have been converted to float.

C. Library Summary

This appendix summarizes library facilities specified, all or in part, in this document.

30 C.1 General utilities <stdlib.h> (ISO §D.11; ANSI §C.11)

```
double atof(const char *nptr);
double strtod(const char *nptr, char **endptr);
float strtof(const char *nptr, char **endptr);
long double strtold(const char *nptr, char **endptr);
```

C.2 Input/output <stdio.h> (ISO §D.10; ANSI §C.10)

```
int fprintf(FILE *stream, const char *format, ...);
int fscanf(FILE *stream, const char *format, ...);
```

C.3 Floating-point <fp.h>

```
45 HUGE_VAL
HUGE_VALF
HUGE_VALL
INFINITY
NAN
FP_NAN
50 FP_INFINITE
```

```
FP_NORMAL
        FP_SUBNORMAL
        FP_ZERO
        fpclassify(floating-expr)
 5
        signbit(floating-expr)
        isfinite(floating-expr)
        isnormal(floating-expr)
        isnan(floating-expr)
        DECIMAL_DIG
10
        float_t
        double_t
        floating-type acos(floating-type x);
        floating-type asin(floating-type x);
        floating-type atan(floating-type x);
15
        floating-type atan2(floating-type y, floating-type x);
        floating-type cos(floating-type x);
        floating-type sin(floating-type x);
        floating-type tan(floating-type x);
        floating-type acosh(floating-type x);
20
        floating-type asinh(floating-type x);
        floating-type atanh(floating-type x);
        floating-type cosh(floating-type x);
        floating-type sinh(floating-type x);
        floating-type tanh(floating-type x);
25
        floating-type exp(floating-type x);
        floating-type exp2(floating-type x);
        floating-type expm1(floating-type x);
        floating-type frexp(floating-type value, int *exp);
        floating-type ldexp(floating-type x, int exp);
30
        floating-type log(floating-type x);
        floating-type log10(floating-type x);
        floating-type log1p(floating-type x);
        floating-type log2(floating-type x);
        floating-type logb(floating-type x);
35
        double modf(double value, double *iptr);
        float modff(float value, float *iptr);
        long double modfl(long double value, long double *iptr);
        floating-type scalb(floating-type x, long int n);
        floating-type fabs(floating-type x);
40
        floating-type hypot(floating-type x, floating-type y);
        floating-type pow(floating-type x, floating-type y);
        floating-type sqrt(floating-type x);
        floating-type erf(floating-type x);
        floating-type erfc(floating-type x);
45
        floating-type gamma(floating-type x);
        floating-type lgamma(floating-type x);
        floating-type ceil(floating-type x);
        floating-type floor(floating-type x);
        floating-type nearbyint(floating-type x);
50
        floating-type rint(floating-type x);
        long int rinttol(long double x);
        floating-type round(floating-type x);
        long int roundtol(long double x);
        floating-type trunc(floating-type x);
55
        floating-type fmod(floating-type x, floating-type y);
        floating-type remainder(floating-type x, floating-type y);
        floating-type remquo(floating-type x, floating-type y, int *quo);
        floating-type copysign(floating-type x, floating-type y);
```

```
double nan(const char *tagp);
        float nanf(const char *tagp);
        long double nanl(const char *tagp);
        floating-type nextafter(floating-type x, long double y);
 5
        float nextafterf(float x, float y);
        double nextafterd(double x, double y);
        long double nextafter1(long double x, long double y);
        floating-type fdim(floating-type x, floating-type y);
        floating-type fmax(floating-type x, floating-type y);
10
        floating-type fmin(floating-type x, floating-type y);
     C.4 Floating-point environment <fenv.h>
       FE_INEXACT
15
       FE_DIVBYZERO
       FE_UNDERFLOW
       FE_OVERFLOW
       FE_INVALID
       FE ALL EXCEPT
20
       FE_TONEAREST
       FE_UPWARD
       FE_DOWNWARD
       FE_TOWARDZERO
       FE_DFL_ENV
25
       fenv_t
       fexcept_t
       void feclearexcept(int excepts);
       void fegetexcept(fexcept_t *flagp, int excepts);
       void feraiseexcept(int excepts);
       void fesetexcept(const fexcept_t *flagp, int excepts);
30
       int fetestexcept(int excepts);
       int fegetround(void);
       int fesetround(int round);
       void fegetenv(fenv_t *envp);
35
       int feholdexcept(fenv_t *envp);
       void fesetenv(const fenv_t *envp);
       void feupdateerv(const fenv_t *envp);
    D. Implementation Limits
40
       §2.3.1 includes supplementary specification for the Standard C component
       #define FLT_ROUNDS
45
       and specification for additional components
       #define _MIN_EVAL_FORMAT
       #define _WIDEST_NEED_EVAL
```

E. Operator / Function Documentation Guide

Adapted from "Documentation of Special Properties of Programs that Compute Elementary Transcendental Functions in the Context of IEEE Standards 754/854 for Floating-Point Arithmetic, with advice for other systems too" (work in progress), by W. Kahan (July 1991).

This appendix previews a forthcoming guide to the documentation of floating-point operators and functions, including most of those in the C language and libraries. For each operator and function, the guide will discuss in detail the prescribed documentation.

"... Read by a system's user, this guide explores many of the issues that could undermine the portability of numerical software if not addressed. Read by a system's implementor, this guide explains what information ought to be supplied and offers a format for its presentation. An implementation's quality can be gauged by the absence of excuses for some of the sad compromises mentioned here. On the other hand, an implementor who resorted to one of those compromises without documenting it might expect users to regard that compromise more as a bug than a feature and to demand its correction.

"Real functions will be dealt with before complex. At first, only the IEEE's default rounding mode to-nearest will be presumed, and only the default responses to exceptions...

"For systems that do not conform to IEEE 754/854, the number ∞, if unavailable, may be approximated by the largest finite number. If no usable -0 is available, use just 0 instead. And if no NaN-like object is available, replace NaN by whatever is the system's usual response to an invalid operation, probably a trap or abortion of execution. Similarly, serious exceptions like overflow and divide-by-zero, if they cannot raise an appropriate flag testable by the program, may have to trap or abort. In any event, serious disruption of a program should be accompanied by a user visible message more informative than, say, a hexadecimal dump. Subnormal numbers, if unusable, must be replaced by zeros with underflow signaled; of course, this signal may be unavailable or practically inaccessible, and hence usually ignored.

"For each function f(x) considered, implementors should supply the following tableau of information:"

40 Invalid Operands

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Invalid operands are those x for which f(x) becomes a new NaN. Example: x < 0 for the square root function.

45 Exact Unexceptional Values

Document these for transcendental functions. Example: $\sin(\pm 0)$ returns ± 0 . f(NaN) returning a NaN need not be included.

50 Exact Exceptional Values

f(x) returns $\pm \infty$ and raises the divide-by-zero exception. Example: $\log(0)$.



Inexact Exceptional Values

Overflow

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f(x) returns $\pm \infty$ and raises the overflow exception.

Underflow

f(x) is subnormal or 0 and raises the underflow exception.

Divide-by-zero

—signaled when f(x) returns $\pm \infty$ though x is only approximately a

pole, e.g. $\tan(\pi/2)$.

Symmetries

10 Like f(-x) == f(x) if f is an even function.

Monotonicity

"(...more important than accuracy!)"

Accuracy

"Accuracy should be described, if not correctly rounded. Accuracy should normally be specified in terms of worst-case error in ulps (units in the last place). (Average error or 20 standard deviation is an abuse of statistics, since worst case error is the killer.) Correctly rounded functions are accurate to within at worst half an ulp; most transcendental functions are very difficult to compute much more accurately than to within less than one ulp. Unfortunately, cases exist for which a kind of backward error-bound may be the best that can be described; this means that the computed value of f(x) may actually be within an ulp or two of f(X) where X is within an ulp or two of the given argument x. Such a bound is acceptable in situations where x is uncertain by a few ulps and uncorrelated with anything else that will be combined with f(x); otherwise such a bound has disagreeable consequences when x comes close to singularities of f, so it is a compromise that should be avoided whenever practical."

Other Noteworthy Properties

"In case correctly rounded is an impracticable accuracy goal, implementations may yet preserve important properties that would be preserved if every computed value were correctly rounded. Some, like monotonicity and symmetry, have already been mentioned; others are inequalities and identities that involve related functions, for instance sqrt (x*x) == fabs(x) absent over/underflow."

F. <fp.h> for IEEE Implementations (ISO §7.5; ANSI \$4.5)

This appendix contains recommended specification of library facilities that is particularly suited for IEEE implementations.

45 The Standard C macro HUGE_VAL and its float and long double analogs, HUGE_VALF and HUGE_VALL, expand to expressions whose values are positive infinities; their evaluations raise no exceptions.

HUGE_VAL could not be implemented as

#define HUGE_VAL (1.0/0.0)

whose use may raise the divide-by-zero exception.

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Special cases for functions in <fp.h> are covered directly or indirectly by the IEEE floating-point standards. The functions sqrt, remainder, rint, and rinttol have direct counterparts in these standards. Appendixes to these standards specify the functions copysign, logb, nextafter, scalb, and nearbyint. The function trunc is equivalent to rint (or, at the implementor's option, to nearbyint) with rounding-toward-zero. The ldexp function is equivalent to the binary version of the scalb function specified in an appendix to the IEEE binary floating-point standard 754. The fmod function is readily derived from the standards' remainder function (see §F.7.1). The other functions are not covered explicitly by the IEEE floating-point standards; however, except as noted, this specification requires that they honor infinities, NaNs, signed zeros, subnormals, and the exception flags in a manner consistent with the basic arithmetic operations covered by the IEEE floating-point standards.

Detectable only through invocation of non-Standard C inquiries or exception handling, the exceptions required here are not in conflict with ISO §7.5.1 (ANSI §4.5.1).

The overflow exception is raised whenever an infinity—or, because of rounding direction, a maximal-magnitude finite number—is returned in lieu of a value whose magnitude is too large. (See §2.)

The underflow exception is raised whenever a result is tiny (essentially subnormal or zero) and suffers loss of accuracy. This NCEG specification for transcendental functions allows raising the underflow (and inexact) exception when a result is tiny and probably inexact.

The IEEE floating-point standards offer the implementation multiple definitions of underflow. All resulting in the same values, the options differ only in that the thresholds when the exception is raised may differ by a rounding error.

According to the IEEE floating-point standards, an enabled underflow trap is taken if the result would be tiny, regardless of loss of accuracy.

The inexact exception is raised whenever the rounded result is not identical to the mathematical result. Except as noted, this NCEG specification for transcendental functions allows raising the inexact exception when a result is *probably* inexact.

For some functions, for example pow, determining exactness in all cases may be too costly.

As implied by §2.2.2, the <fp.h> functions do not raise spurious exceptions (detectable by the user). For example, the implementation must hide an underflow generated by an intermediate computation of a non-tiny result.

Whether transcendental functions honor the rounding direction mode and any rounding precision mode is implementation-defined.

Generally, one-parameter functions of a NaN argument return that same NaN and raise no exception. (See §3.1.1.1.)

For the Standard C <math.h> functions, the specification in the subsections of §F.1 appends to the Standard C definitions. For the NCEG extensions, it appends to the definitions in §4.3 of this document.

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Trigonometric functions (ISO §7.5.2; ANSI §4.5.2) F.1

F.1.1 The acos function (ISO §7.5.2.1; ANSI §4.5.2.1)

floating-type acos(floating-type x); 5

• acos (1) returns +0.

• acos (x) returns a NaN and raises the invalid exception for |x| > 1.

10 F.1.2 The asin function (ISO §7.5.2.2; ANSI §4.5.2.2)

floating-type asin(floating-type x);

• asin (± 0) returns ± 0 .

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40

• as in (x) returns a NaN and raises the invalid exception for |x| > 1.

F.1.3 The atan function (ISO §7.5.2.3; ANSI §4.5.2.3)

floating-type atan(floating-type x);

atan (±0) returns ±0.

• atan (\pm INFINITY) returns $\pm \pi/2$.

F.1.4 The atan2 function (ISO §7.5.2.4; ANSI §4.5.2.4)

floating-type atan2(floating-type y, floating-type x);

 If one argument is a NaN then atan2 returns that same NaN; if both arguments are NaNs then atan2 returns one of its arguments.

• atan2 $(\pm 0, x)$ returns ± 0 , for x > 0.

• atan2 $(\pm 0, +0)$ returns ± 0 .

• atan2 (± 0 , x) returns $\pm \pi$, for x < 0.

• atan2 (± 0 , -0) returns $\pm \pi$.

• atan2(y, ± 0) returns $\pi/2$ for y > 0.

• atan2(y, ± 0) returns $-\pi/2$ for y < 0.

• atan2 ($\pm y$, INFINITY) returns ± 0 , for finite y > 0.

• atan2 (±INFINITY, x) returns ±\pi/2, for finite x.

• atan2 ($\pm y$, -INFINITY) returns $\pm \pi$, for finite y > 0.

• atan2(\pm INFINITY, INFINITY) returns $\pm \pi/4$. • atan2(\pm INFINITY, -INFINITY) returns $\pm 3\pi/4$.

The more contentious cases are y and x both infinite or both zeros. See [7] for a justification of the choices above.

45 atan2 (y, 0) does not raise the divide-by-zero exception, nor does atan2 (0, 0) raise the invalid exception.

F.1.5 The cos function (ISO §7.5.2.5; ANSI §4.5.2.5)

50 floating-type cos(floating-type x);

• cos (±INFINITY) returns a NaN and raises the invalid exception.

```
F.1.6 The sin function (ISO §7.5.2.6; ANSI §4.5.2.6)
       floating-type sin(floating-type x);
       • sin(\pm 0) returns \pm 0.
 5
       • sin (±INFINITY) returns a NaN and raises the invalid exception.
    F.1.7 The tan function (ISO §7.5.2.7; ANSI §4.5.2.7)
10
       floating-type tan(floating-type x);
       • tan(\pm 0) returns \pm 0.
       • tan (±INFINITY) returns a NaN and raises the invalid exception.
          Hyperbolic functions (ISO §7.5.3; ANSI §4.5.3)
15
    F.2.1 The acosh function
       floating-type acosh(floating-type x);
20
       • acosh(1) returns +0.
       • acosh(+INFINITY) returns +INFINITY.
       • acosh (x) returns a NaN and raises the invalid exception if x < 1.
    F.2.2 The asinh function
25
       floating-type asinh(floating-type x);
       • asinh(\pm 0) returns \pm 0.
       • asinh(±INFINITY) returns ±INFINITY.
30
    F.2.3 The atanh function
       floating-type atanh(floating-type x);
35
       • atanh(±0) returns ±0.
       • atanh(±1) returns ±INFINITY.
       • atanh (x) returns a NaN and raises the invalid exception if |x| > 1.
    F.2.4 The cosh function (ISO §7.5.3.1; ANSI §4.5.3.1)
40
       floating-type cosh(floating-type x);
       • cosh(±INFINITY) returns + INFINITY.
45
    F.2.5 The sinh function (ISO §7.5.3.2; ANSI §4.5.3.2)
       floating-type sinh(floating-type x);
50
       • sinh(\pm 0) returns \pm 0.
       • sinh (±INFINITY) returns ±INFINITY.
```

```
F.2.6 The tanh function (ISO §7.5.3.3; ANSI §4.5.3.3)
                   floating-type tanh(floating-type x); was a said and a said a said
   5
                   • tanh (±0) returns ±0.
                   • tanh (±INFINITY) returns ±1. Will sell beaut box Maid a actually overselve at a large
                         Exponential and logarithmic functions (ISO §7.5.4; ANSI
                                                                                                                                                                $4.5.4)
 10
           F.3.1 The exp function (ISO §7.5.4.1; ANSI §4.5.4.1)
                   floating-type exp(floating-type x);
                  • exp(+INFINITY) returns +INFINITY.
 15
                  • exp(-INFINITY) returns +0.
           F.3.2 The exp2 function
20
                  floating-type exp2(floating-type x);
                  • exp2(+INFINITY) returns +INFINITY.
                  exp2(-INFINITY) returns +0.
25
           F.3.3 The expm1 function
                  floating-type expm1(floating-type x);
                  • expm1(\pm 0) returns \pm 0.
30
                  expm1(+INFINITY) returns +INFINITY.
                  • expm1(-INFINITY) returns -1.
           F.3.4 The frexp function (ISO §7.5.4.2; ANSI §4.5.4.2)
35
                  floating-type frexp(floating-type value, int *exp);
                  • frexp(±0, exp) returns ±0, and returns 0 in *exp.

    frexp(±INFINITY, exp) returns ±INFINITY, and returns an unspecified value in

                 • frexp of a NaN argument is that same NaN, and returns an unspecified value in
                 • Otherwise, frexp raises no exception.
                 On a binary system, frexp is equivalent to the comma expression
                         ( (*exp = (value == 0) ? 0 : (int)(1 + logb(value))),
                               scalb(value, -(*exp)) )
                         The Idexp function (ISO §7.5.4.3; ANSI §4.5.4.3)
                 floating-type ldexp(floating-type x, int exp);
                On a binary system, 1dexp is equivalent to
```

40

45

```
scalb(x, exp)
            Note that ldexp may not provide the full functionality of scalb for extended values,
            because the power required to scale from the smallest (subnormal) to the largest extended
            value exceeds the minimum INT_MAX allowed by Standard C.
 5
     F.3.6 The log function (ISO §7.5.4.4; ANSI §4.5.4.4)
         floating-type log(floating-type x);
10
         • log(±0) returns -INFINITY and raises the divide-by-zero exception.
         • log(x) returns a NaN and raises the invalid exception if x < 0.
         • log(+INFINITY) returns +INFINITY.
     F.3.7 The log10 function (ISO §7.5.4.5; ANSI §4.5.4.5)
15
         floating-type log10(floating-type x);
         • log10(±0) returns -INFINITY and raises the divide-by-zero exception.
         • log10(x) returns a NaN and raises the invalid exception if x < 0.
20
         • log10(+INFINITY) returns +INFINITY.
     F.3.8
             The log1p function
25
         floating-type log1p(floating-type x);
         • log1p(\pm 0) returns \pm 0.
         • log1p(-1) returns -INFINITY and raises the divide-by-zero exception.
         • log lp(x) returns a NaN and raises the invalid exception if x < -1.
30
         • log1p(+INFINITY) returns +INFINITY.
     F.3.9 The log2 function
         floating-type log2(floating-type x);
35
         • log2 (±0) returns -INFINITY and raises the divide-by-zero exception.
         • log2(x) returns a NaN and raises the invalid exception if x < 0.
         • log2(+INFINITY) returns +INFINITY.
     F.3.10 The logb function
40
         floating-type logb(floating-type x);
         • logb(±INFINITY) returns +INFINITY.
         • logb(±0) returns -INFINITY and raises the divide-by-zero exception.
45
               The modf functions (ISO §7.5.4.6; ANSI §4.5.4.6)
      F.3.11
         double modf(double value, double *iptr);
50
         float modff(float value, float *iptr);
         long double modfl(long double value, long double *iptr);
         • modf (value, iptr) returns a result with the same sign as the argument value.
         • modf (±INFINITY, iptr) returns ±0 and stores ±INFINITY through iptr.
55
         • modf of a NaN argument returns that same NaN and also stores it through iptr.
```

January 6, 1994

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```
modf behaves as though implemented by
```

```
#include <fenv.h>
#include <fp.h>
#pragma fenv_access on
double modf(double value, double *iptr)

{
    int save_round = fegetround();
    fesetround(FE_TOWARDZERO);
    *iptr = nearbyint(value);
    fesetround(save_round);
    return copysign(
        (fabs(value) == INFINITY) ? 0.0 : value - (*iptr),
        value);
}
```

F.3.12 The scalb function

```
20 floating-type scalb(floating-type x, long int n);
```

• scalb(x, n) returns x if x is infinite, zero, or a NaN.

• scalb handles overflow and underflow like the basic IEEE standard arithmetic operations.

F.4 Power and absolute value functions (ISO §7.5.5, 7.5.6; ANSI §4.5.5, 4.5.6)

F.4.1 The fabs function (ISO §7.5.6.2; ANSI §4.5.6.2)

```
floating-type fabs(floating-type x);
```

- fabs (±0) returns +0.
- fabs (±INFINITY) returns +INFINITY.

F.4.2 The hypot function

```
floating-type hypot(floating-type x, floating-type y);
```

- hypot(x, y), hypot(y, x), and hypot(x, -y) are equivalent.
- hypot (x, y) returns + INFINITY if x is infinite.
- If both arguments are NaNs then hypot returns one of its arguments; otherwise, if x is a NaN and y in not infinite then hypot returns that same NaN.
- hypot (x, ±0) is equivalent to fabs (x).

Note that hypot (INFINITY, NAN) returns +INFINITY, under the justification that hypot (INFINITY, y) is +INFINITY for any numeric value y.

F.4.3 The pow function (ISO §7.5.5.1; ANSI §4.5.5.1)

floating-type pow(floating-type x, floating-type y);

- pow(x, ±0) returns 1 for any x.
- pow(x, +INFINITY) returns +INFINITY for |x| > 1.

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45

```
• pow(x, +INFINITY) returns +0 for |x| < 1.
         • pow(x, -INFINITY) returns +0 for |x| > 1.
         • pow(x, -INFINITY) returns +INFINITY for |x| < 1.
         • pow(+INFINITY, y) returns +INFINITY for y > 0.
         • pow(+INFINITY, y) returns +0 for y < 0.
 5
         • pow(-INFINITY, y) returns -INFINITY for y an odd integer > 0.
         • pow(-INFINITY, y) returns + INFINITY for y > 0 and not an odd integer.
         • pow(-INFINITY, y) returns -0 for y an odd integer < 0.
         • pow(-INFINITY, y) returns +0 for y < 0 and not an odd integer.
         • pow(x, y) returns one of its NaN arguments if y is a NaN, or if x is a NaN and y is
10
         • pow(±1, ±INFINITY) returns a NaN and raises the invalid exception.
         • pow(x, y) returns a NaN and raises the invalid exception for finite x < 0 and finite
         nonintegral y.
         • pow (\pm 0, y) returns \pm 1NFINITY and raises the divide-by-zero exception for y an odd
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         integer < 0.
         • pow (\pm 0, y) returns + INFINITY and raises the divide-by-zero exception for y < 0,
         finite, and not an odd integer.
         • pow(\pm 0, y) returns \pm 0 for y an odd integer > 0.
20
         • pow (\pm 0, y) returns +0 for y > 0 and not an odd integer.
             See [7].
             pow(NaN, 0). [7] provides extensive justification for the value 1. An opposing point of
             view is that any return value of a function of a NaN argument should be a NaN, even if the
25
             function is independent of that argument—as, in the IEEE floating-point standards,
             NAN <= +INFINITY is false and raises the invalid exception.
     F.4.4 The sqrt functions (ISO §7.5.5.2; ANSI §4.5.5.2)
30
         floating-type sqrt(floating-type x);
         sqrt is fully specified as a basic arithmetic operation in the IEEE floating-point
         standards.
35
            Error and gamma functions
     F.5.1
             The erf function
40
         floating-type erf(floating-type x);
         • erf (\pm 0) returns \pm 0.
         • erf(±INFINITY) returns ±1.
45
      F.5.2 The erfc function
         floating-type erfc(floating-type x);
         • erfc(+INFINITY) returns +0.
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         • erfc(-INFINITY) returns 2.
     F.5.3 The gamma function
```

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floating-type gamma(floating-type x);

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```
• gamma (+INFINITY) returns +INFINITY.
   • gamma (x) returns a NaN and raises the invalid exception if x is a negative integer or
   • gamma (-INFINITY) returns a NaN and raises the invalid exception.
F.5.4 The lgamma function
   floating-type lgamma(floating-type x);
   • lgamma (+INFINITY) returns +INFINITY.
   • 1gamma (x) returns + INFINITY and raises the divide-by-zero exception if x is a
   negative integer or zero.
   • 1gamma (-INFINITY) returns a NaN and raises the invalid exception.
F.6
      Nearest integer functions (ISO §7.5.6; ANSI §4.5.6)
      The ceil function (ISO §7.5.6.1; ANSI §4.5.6.1)
   floating-type ceil(floating-type x);
   • ceil(x) returns x if x is ±INFINITY or ±0.
   The double version of ceil behaves as though implemented by
      #include <fenv.h>
      #include <fp.h>
      #pragma fenv_access on
      double ceil(double x)
         double result;
         int save_round = fegetround();
         fesetround(FE_UPWARD);
         result = rint(x); /* or nearbyint instead of rint */
         fesetround(save_round);
         return result;
     The floor function (ISO §7.5.6.3; ANSI §4.5.6.3)
  floating-type floor(floating-type x);
```

• floor(x) returns x if x is ±INFINITY or ±0.

45 See the sample implementation for ceil in §F.6.1.

F.6.3 The nearbyint function

floating-type nearbyint(floating-type x);

The nearbyint function differs from the rint function only in that the nearbyint function does not raise the inexact flag.

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F.6.4 The rint function

```
floating-type rint(floating-type x);
```

The rint function use IEEE standard rounding according to the current rounding direction. It raises the inexact exception if its argument differs in value from its result.

F.6.5 The rinttol function

10 long int rinttol(long double x);

The rinttol function provides floating-to-integer conversion as prescribed by the IEEE standards [2], [3] §5.4. It rounds according to the current rounding direction. If the rounded value is outside the range of long int, the numeric result is unspecified and the invalid exception is raised. When it raises no other exception and its argument differs from its result, rinttol raises the inexact exception.

F.6.6 The round function

floating-type round(floating-type x);

The double version of round behaves as though implemented by

```
#include <fenv.h>
25
           #include <fp.h>
           #pragma fenv_access on
           double round(double x) {
              double result;
              fenv_t save_env;
30
              feholdexcept(&save_env);
              result = rint(x);
              if (fetestexcept(FE_INEXACT)) {
                  fesetround(FE_TOWARDZERO);
                 result = rint(copysign(0.5 + fabs(x), x));
35
              feupdateenv(&save env);
              return result:
           }
```

40 round may but is not required to raise the inexact exception for nonintegral numeric arguments, as this implementation does.

F.6.7 The roundtol function

45 long int roundtol(long double x);

roundtol differs from rinttol with the default rounding direction just in that roundtol (1) rounds halfway cases away from zero and (2) may but need not raise the inexact exception for nonintegral arguments that round to within the range of long int.

F.6.8 The trunc function

floating-type trunc(floating-type x);

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The trunc function uses IEEE standard rounding toward zero (regardless of the current rounding direction).

F.7 Remainder functions (ISO §7.5.6; ANSI §4.5.6)

F.7.1 The fmod function (ISO §7.5.6.4; ANSI §4.5.6.4)

floating-type fmod(floating-type x, floating-type y);

• If one argument is a NaN then fmod returns that same NaN; if both arguments are NaNs then fmod returns one of its arguments.

• fmod (±0, y) returns ±0 if y is not zero.

• fmod (x, y) returns a NaN and raises the invalid exception if x is infinite or y is zero.

• fmod(x, ±INFINITY) returns x if x is not infinite.

The double version of fmod behaves as though implemented by

F.7.2 The remainder function

floating-type remainder(floating-type x, floating-type y);

remainder is fully specified as a basic arithmetic operation in the IEEE floating-point standards.

F.7.3 The remquo function

floating-type remquo(floating-type x, floating-type y, int *quo);

remquo follows the specification for remainder. It has no further specification special to IEEE implementations.

F.8 Manipulation functions

F.8.1 The copysign function

floating-type copysign(floating-type x, floating-type y);

copysign is specified in appendices to the IEEE floating-point standards. It has no specification special to IEEE implementations.

F.8.2 The nan functions

double nan(const char *tagp);
float nanf(const char *tagp);
long double nanl(const char *tagp);

All IEEE implementations support quiet NaNs, hence declare all the nan functions.

F.8.3 The nextafter functions

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floating-type nextafter(floating-type x, long double y);
float nextafterf(float x, float y);
double nextafterd(double x, double y);
long double nextafterl(long double x, long double y);

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- If one argument is a NaN then nextafter returns that same NaN; if both arguments are NaNs then nextafter returns one of its arguments.
- nextafter (x, y) raises the overflow and inexact exceptions if x is finite and the function value is infinite.
- nextafter (x, y) raises the underflow and inexact exceptions if the function value is subnormal and x != y.

F.9 Maximum, minimum, and positive difference functions

25 F.9.1 The fdim function

floating-type fdim(floating-type x, floating-type y);

• If one argument is a NaN then fdim returns that same NaN; if both arguments are NaNs then fdim returns one of its arguments.

F.9.2 The fmax function

floating-type fmax(floating-type x, floating-type y);

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• If just one argument is a NaN then fmax returns the other argument; if both arguments are NaNs then fmax returns one of its arguments.

fmax might be implemented as

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```
isnan(y) ? x : (y ! <= x ? y : x)
```

Ideally, fmax would be sensitive to the sign of zero, for example fmax(-0.0, +0.0) should return +0; however, implementation in software may be impractical.

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Some applications may be better served by a *max* function that would return a NaN if one of its arguments were a NaN:

```
isnan(y) ? y : (y !> x ? x : y)
```

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Note that two branches still are required, for symmetry in NaN cases.

F.9.3 The fmin function

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floating-type fmin(floating-type x, floating-type y);
fmin is analogous to fmax. See §F.9.2.

X3J11.1 Ballot Comments

- At its May 1993 meeting, NCEG voted on the motion to forward "Floating-Point C 5 Extensions" to its parent committee, X3J11. The results were 7 yes 2 ves with comments 10 1 no with comments This section contains the comments that accompanied the two yes-with-comments and one no-with-comments votes. Author's responses are in italics. 15 Subject: Comments on NCEG paper X3J11.1/93-001 Floating-Point C Extensions Vote: Yes, with comment. 20 The following are IBM's comments to be included with the X3 subgroup letter ballot on X3J11.1/93-001 as amended by 93-022. A general comment based upon 26. Miscellanea compiled by Rex Jaeschke 25 pages 248-249. The Journal of C Language Translation, Volume 3, Number 3, December, 1991. All dummy argument identifier names used in the C Standard are non-conforming! Essentially, these identifiers must either be omitted, spelled with a leading underscore and a capital letter, or with two leading underscores. Therefore, you need to change 30 all your function prototypes. IBM votes for adding "__" to the names. To see why the current prototypes fail, consider: #define x 3 #include <math.h> #define stream 3 35 #include <stdio.h> An alternative is to add the following paragraph after page 4, line 7: As in the C Standard, function prototypes are shown with dummy argument identifier names in the user's name space. The real 40 prototypes in the various headers would either omit the identifier, or add a leading '_' and capitalize the first letter, or add two leading '_'s to the identifier. For example, double modf(double value, double *iptr); would be done as one of 45 double modf(double, double *); double modf(double _Value, double *_Iptr); double modf(double __value, double *__iptr);
- The document follows the approach of Standard C in documenting the libraries in a more readable style than could appear in real header files.

A second general comment: The Floating-Point Environment is not well defined and is incomplete. From section 4.4 Floating-Point Environment, fesetexcept and fesetenv set, but not raise, exceptions. Therefore, set cannot mean the same thing as raised. Therefore, there must be at least 3 states (set, raised, cleared) for each exception.

Since 3-state is hard to do on a binary machine, it appears that each exception has associated with it:

Set or cleared

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2) Raised or not raised

- 3) Trap enabled or disabled
- 4) Optional information, such as:
 - a) Address of the code which raised it
- Given that a distinction has been made between set and raised, the functions in section 4.4 are not complete. There is no way to test what exceptions are currently raised. There is no way to remove a raised exception. The only way to restore the entire floating-point environment is to feclear except (FE_ALL_EXCEPT); followed by

feupdateenv(&save_env);

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One issue not addressed is how long is an exception raised?

Each exception flag has just two states: set and clear.

The act of raising an exception is the typical means by which an exception flag becomes set. Arithmetic operations and the feraiseexcept function raise exceptions. On the other hand, the functions festexcept and festenv restore flag state captured by prior calls to fegetexcept and fegetenv, respectively. Within this specification, an exception flag cannot become set until it has been raised.

Now, for the specific comments.

- Page 4, line 37, Section 1.5 Definition of Terms, refers to "status flags" and "control modes", yet neither are defined. So, the next items are needed.
- Page 4, line 9, need to add something like:

 Control modes -- variables that the user may set, sense, save, and restore to control the execution of subsequent arithmetic operations. Floating-point control mode is made up of at least the rounding direction mode and the rounding precision mode. An implementation may also have traps disabled/enabled modes (which is not covered by this specification).
- Page 4, line 51, Mode:
 Add at end of sentence: See control modes.
- Page 5, line 32, need to add something like:

 Status flag -- a flag signifying that a floating-point exception has occurred since the user last cleared it (each flag may take three states: set, raised and clear). When not cleared, a status flag may contain additional system-dependent information, possibly inaccessible to some users. IEEE implementations support overflow, underflow, invalid, divide-by-zero, and inexact status flags.

Another choice for this is status flags is made up of exception flags (raised/not raised) and 'sticky' accrued flags (set/cleared).

- The terms control and status are intentionally allowed more general interpretation than the suggested definitions, which apply specifically to their use in the IEEE floating-point standards.
- Page 15, lines 37-39, Section 3.2.1 Floating and integral

 This whole paragraph needs to be reworked for two reasons. First, it is possible that infinity and/or NaN could be represented in the integer type; in that case there should not be an exception.

 Second, it is possible that for overflow there is an INTEGER overflow exception that could be raised or signaled instead of a FLOATING-POINT invalid operation exception. IEEE-754, page 14, section 7.1 Invalid Operation, item (7) says: "Conversion of a binary floating-point number to an integer or decimal format when overflow, infinity or NaN precludes a faithful representation in that format and this cannot otherwise be signaled."

Consistent treatment of NaN or infinity values for integer types seems inconsistent with the Standard C's specification for those types. Even if implementation were possible, program portability would argue for a single model for raising exceptions in these cases.

Page 26, line 39, Section 4.2.1.2 The strtof, strtod, and strtold functions:

There is a difference between translation-time and execution-time with respect to the number of characters (digits) in a number and that might impact conversion. ANSI C 2.2.4.1, page 14, line 17 has the minimum limit of 509 characters in a logical source line and line 19 has 32767 bytes in an object (such as the string passed to strtod). So the string ".000...0001e32759" that is 32767 bytes long (... is around 32755 0's) might convert to the value 0.0 if only the first 509 digits are used, but convert to the value 1.0 if the full 32767 digits are used. The same difference might also apply to the scanf family.

The intention is that translation-time and execution-time conversion match when both are within their respective limits.

Page 27, line 11, Section 4.2.1.2 The strtof, strtod, and strtold functions:

Is an implementation that supports sign-opt NANS(n-char-sequence-opt) or sign-opt NANS, for signaling NaNs, in violation of this standard?

If so, than these two syntax forms need to be added. If not, then a note should be added after line 26 on page 27 explaining that implementations may be extended to support signaling NaNs, and that the above is the syntax. NCEG should at least standardize the syntax of signaling NaNs.

Signaling NaNs are not included in the specification. The value of the suggested partial specification does not seem to justify the added complexity to the document.

Page 48, lines 27-28, Section 4.3.9.2 The nan functions:

Swap these two lines, so the float comes first. This will then be consistent with 4.3.4.11 modf functions on page 41.

This has been addressed in Draft 2 of the technical report.

40 Page 53, line 44, Section 4.4.1.4 The fesetexcept function: Change "must" to "should".

"Must" is consistent with the fact that certain behavior is otherwise undefined.

Page 60, line 5, Section B.1 Expression evaluation: What is the rational[e] for the statement that exceptions need not be precise?

Making them precise is impractical on some hardware, especially relative to the value of doing so.

Page 67, line 23, Section F. <fp.h> for IEEE Implementations: Change 'is' to 'should be' or 'is probably'. IBM would like to allow inexact to not be raised in some cases. That is, we would like inexact to probably be raised when it should be raised.

The suggested change is inconsistent with the IEEE floating-point specification for basic operations.

Page 67, line 40, Section F. <fp.h> for IEEE Implementations

Does "appends to" mean that errno support is required? I believe
that NCEG wants errno support removed or optional. But, I am
afraid that someone may interpret this area as still requiring
support for errno.

This specification is not intended of itself to require, or prohibit, support for errno.

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Page 73, line 11, Section F.4.3 The pow function:

Add rational[e] for why pow(+1, +/- INFINITY) is NaN, instead of +1.

- 5 The document generally does not provide rationale for such cases, which are based on a straightforward application of limits.
- Fred Tydeman, IBM, Austin, Texas (512) 838-3322; fax (512) 838-3484

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Meyers comment was: "The problem with strtof and HUGE_VAL is a systematic problem with the library functions, and the correction is to add float and long double versions of HUGE_VAL."

This has been addressed in Draft 2 of the technical report.

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From: Tom MacDonald -- Cray Research Inc.

Subject: CRI's comments on X3J11.1/93-001

Vote: No with comment

Cray Research does not support the forwarding of document X3J11.1/93-001 dated Jan. 20, 1993 to be sent to our parent committee, X3J11, for the reasons listed below. If these issues are addressed to our satisfaction, we will change our position and vote Yes.

1) Pragmas

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- It is a mistake to specify any pragmas in this document. They cannot be used in macros and are intended for implementation specific needs. One possibility is introduce new macros that accept ON/OFF/DEFAULT arguments and expand into implementation specific directives or keywords. This can be hidden in a header file such as the proposed <fp.h> header.
 - Replacing the pragmas with macros, though requiring a fairly large number of editorial changes, appears to be straightforward. At its May 92 meeting, X3J11.1 considered such a proposal but was reluctant to make the change without additional review. If X3J11 desires the change, it could be made easily and with no loss of facility.
- 45 2) New relational and equality operators

The proposed new relational operators are of questionable utility. These operators are: !<>=, <>, <>=, !<=, !<, !>=, !>, and !<>. These new operators are intended to provide additional support for NaNs. However, the `isnan' macro in conjunction with the equality operators (== and !=) are more than adequate for NaN support. For example:

```
isnan(X) /* means X is a NaN */
X!=X /* means X is a NaN */

X==X /* means X is not a NaN */
```

The most common coding style is to check a function's arguments upon entry, and if any are NaNs, error processing occurs. There is insufficient justification for adding all of these new operators.

In contrast the addition of the new operators makes C a more complicated language. This proposal more than doubles the number of relational and equality operators. The following table shows how much the complexity of

comparisons increases with these new operators.

Standard	C	Comparisons
The second		

	less	equal	greater
<	T	F	on IAF
<=	T	T	F
>	F	F	T
>=	F	T	T
! =	T	F	T
==	F	T	F
	<= > >=	< T T T T T T T T T T T T T T T T T T T	< T F < T T

Proposed IEEE Comparisons

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		less	equal	greater	unordered
	<	T	F	F	F
25	<=	T	T	F	F
	>	F	F	T	F
	>=	F	T	T	F
	! =	T	F	T	T
30	==	F	T	F	F
	!<	F	T	T	T
	!<=	F	F	T	T
	!>	T	T	F	T
	!>=	T	F	F	T
35	!<>	F	T	F	T
	<>	T	F	T	F
	<>=	T	T	T	F
	!<>=	F	F	F	T

The number of possible comparisons increases from 18 to 56.

Another issue is the precedence of the new operators. The proposal states that they have the same precedence as the relational operators when clearly some of the new operators are more closely tied to equality operations (e.g., !<>). This only emphasizes that the new operators obscure the meaning of the terms 'equality' and 'inequality' thereby making algorithms less clear.

A final issue is that the use of some of these new operators with integer and pointer types is nonsensical (i.e., !<>= and <>=). The non-symmetric nature with respect to types is both confusing and troubling.

Rationale in §3.3.2 offers justification for the new operators.

3) Types and portability of code

The proposal states:

"The long double type should have strictly more precision than double which should have at least twice the number of digits of precision as float. If not, the implementation should emit a warning when processing a translation unit that uses distinct floating types with the same precision."

Even though this is only a "should", we think it is an unnecessary and

misleading suggestion. It is unnecessary because as long as the types used have at least the minimum amount of precision required by the algorithm, the result will be accurate to within the ability of the type to represent the true result. Forcing the distinct types to have 5 different amounts of precision does not contribute to the accuracy. And it is misleading because it suggests that code will be completely portable (that is, give the exact same results) between all implementations that conform with the proposed standard. This is not true. The document is riddled with "implementation defined" specifications. Almost any of these 10 open the door for slightly different results in different implementations. So either all aspects of precision and evaluation methods have to be precisely and unambiguously defined and required or the goal of absolute portability must be forgotten. It is not realistic to force all implementations to just one hardware model, therefore, variations in 15 results must be expected.

The recommendation acknowledges programs that depend on the prescribed relationships among types but nonetheless enjoy a level of portability.

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